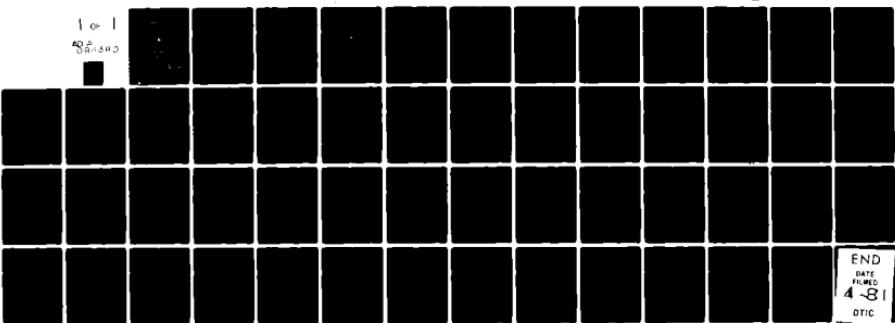


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NAVAL OBSERVATORY WASHINGTON DC TIME SERVICE DIV  
EVALUATION OF PREDICTABILITY OF QUARTZ-CRYSTAL OSCILLATORS AND --ETC(U)  
JAN 81 L G CHARRON, R T CLARKE  
MIPR-HC1001-8-40079  
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### EVALUATION OF PREDICTABILITY OF QUARTZ-CRYSTAL OSCILLATORS AND OTHER DEVICES

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| 19. ABSTRACT (Continue on reverse side if necessary and identify by block number)<br>Data were collected over varying intervals for several types of devices (quartz-crystal, rubidium, cesium beam oscillators and hydrogen maser) and compared to NAVOBSY USNO MC. An ARIMA and several polynomial models for prediction purposes were evaluated. It is concluded that very simple prediction methods can suffice in maintaining a timing system. |                                     |                                                                                  |  |

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# U.S. NAVAL OBSERVATORY



## EVALUATION OF PREDICTABILITY OF QUARTZ-CRYSTAL OSCILLATORS AND OTHER DEVICES

FEBRUARY 1981

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## INTRODUCTION

The work to be discussed in this report has resulted from the following:

- a. The recent discovery that Autoregressive Integrated Moving Average (ARIMA) models can be applied in the representation of the statistics of clock behavior, and that this can lead to a better separation of purely random from systematic clock noise;
- b. The desire to replace cesium beam atomic clocks with less expensive devices in those applications where frequent comparisons with an external reference are possible; and
- c. The recent availability of superior quartz crystal clocks and microprocessors at relatively low cost.

The use of ARIMA routines for clock modelling had originally been proposed by Barnes (reference 1). At that time, it was not believed to be a practical model because of the extraordinary precision with which the higher coefficients had to be determined in order to achieve acceptable results. The user of higher order polynomials for extrapolation purposes also has this difficulty. In both cases the available data simply does not allow determination of coefficients. This inability produces a compounded effect as extrapolation time goes beyond a few days. In time, even a third power polynomial as a representation of a frequency drift is useless in the case of cesium clocks unless the drift is based on several months of data. However, Percival (reference 2) has showed that for shorter intervals which are important in most practical applications it is not necessary to use such complicated procedures. The question then arises whether these newer predicting models will not allow an extrapolation of quartz crystal clocks for a few days in a simple and reliable manner. For a general discussion of the problem in separation of systematics from purely random (white) clock noise, see reference 3 and particularly figure 3 in reference 4.

The second issue, the replacement of expensive clocks, has also been considered previously. Current digital techniques and, particularly, the availability of inexpensive microprocessors now necessitate consideration of replacing hardware phase-lock loops with processor-controlled phase-steppers. Once data has been obtained from an oscillator connected to an external reference, digital filtering offers a sophisticated way of extrapolating beyond that data whenever the external reference is unavailable. For a general introduction to digital filtering, see reference 5.

The principal idea of using ARIMA models for this purpose is explained on p. 380 of reference 4. An ARIMA model ( $p, d, q$ ) is a model with  $p$  regression and  $q$  moving average coefficients in the representation of the  $d$ -th differences of clock errors.

Suppose we represent these second differences in time (this yields a stationary time series, in contrast to the series of frequencies which usually exhibit drifts) by a linear difference equation such as:

$$z(t) = \sum_{i=1}^p \theta_i \cdot z(t-i) + \sum_{j=1}^q \phi_j \cdot a(t-j) + D_0 + a(t)$$

where the  $\theta$ 's represent regression coefficients and the  $D$ 's smoothing coefficients. The  $a$ 's then represent the purely random part of the noise, i.e., the one-step advance prediction errors. The  $D_0$  term (if it can be determined with sufficient confidence) is the systematic drift. Considering the purpose of this investigation, i.e., a study of the feasibility of using simple routines in field applications, it is noteworthy that after considerable experimentation with different choices of models and parameters it has become obvious that the simplest model, the ARIMA (0,2,1) with a coefficient of 0.75 as smoothing parameter is best for the purpose desired. The criteria used was that of a least square solution. In no case has a drift coefficient been included. The above equation therefore reduces to:

$$z(t) = -0.75 \cdot a(t-1) + a(t)$$

where the  $z(t)$  are the second differences of oscillator phase.

Another general comment should be made. For several years, it has been a common complaint that system designers could not relate to the stability measure which is most commonly used, the two-sample (Allan) variance. Indeed, as pointed out in reference 2, the use of this measure is not without problems. While the two-sample variance (and its square root, which corresponds to a standard deviation) is very simple to obtain, it is not completely insensitive to the presence of noise concentrated in narrow (Fourier) spectral regions; i.e., it is a measure which depends on the presence of a power low-noise spectrum. In contrast, the prediction errors obtained in this report are by themselves a measure of clock performance which is completely independent of any theory. It depends only on the choice of the prediction model. In this way, we obtain a measure which gives the designer exactly what is needed in any practical application.

#### DISCUSSION OF MEASUREMENTS

Table 1 lists the devices for which measurements were made using the data acquisition system (DAS) of the U.S. Naval Observatory (USNO) which was described by Putkovich (reference 6). [Specifications for the URQ10 and the Disciplined Time Frequency Oscillator (DTFO) are given in Appendix A. Specifications for the other devices are available in the manufacturers' manuals.] In this system, a matrix of clock starts against clock stops is measured with a time interval counter (HP5360 Computing Counter) with a resolution of 100ps. The measurements are performed every hour and form the basis for all time scale computations. The main advantage of this system is that the measurements, since they are time interval measurements, are strictly linear and are not plagued by nonlinearities of phase meters, etc. However, if 5MHz signals are used directly and the zero cross-overs are adopted as time markers, cycle ambiguities, of 200ns may exist. This is of no concern in the case of atomic clocks, but crystal clocks exhibit large frequency (rate) differences and the cycle adjustments cannot always be made unambiguously. As a consequence, only the 1 pps measurements are considered completely authoritative for the crystal clocks. This problem is peculiar to the data collection method and not at all representative of a real-life situation where code generators would be driven from the oscillators. After adjustment for cycle slips and other discontinuities, the value of 0000 UT has been used in the various solutions.

In some cases, there have been periods when it became obvious that the clock under test had suffered a disturbance (such as breakdown of laboratory temperature control). Such obviously disturbed periods for any clock have been excluded from analysis since the extrapolation of precise time measurements would not be representative of the capability of that clock. Figures 1 through 15 present UTC (USNO, MC) minus UTC (device).

The prediction errors have all been computed as the root mean square (rms) difference between a specific model prediction and the actual clock error as measured after the fact. These values, as well as the number of samples upon which they were based, are presented in tables 2 through 19. For these purposes, it is clear that the confidence in the prediction errors so determined will increase the longer the total data run.

Figures 16 and 17 are plots of the rms error versus prediction lead time for the shortest and longest calibration interval as determined by the ARIMA model for the URQ10 crystal oscillator and the HP236 rubidium. These are graphic representations of the data contained in tables 4 and 8. As anticipated, discontinuities are introduced when the number of sample intervals change. An extreme case is seen for URQ10 for the calibration interval of 56 days; between days 25 and 26 the number of sample intervals changes from 7 to 8.

In general, one can see from the tables that prediction errors decrease as the calibration interval increases. However, in all cases one can observe that there is a definite limit beyond which the prediction errors do not improve with longer calibration intervals. At this point, it would be necessary to change models. In the case of cesiums, at least, reference 2 gives several examples of (1,2,1) and (0,2,2) models which give very small prediction errors for 64 days. In the context of this investigation, however, direct comparability is judged the most important goal and the most interesting lead times for practical applications will be short ones.

The quality of the clock considered is directly given by its predictability. However, the manner in which the prediction errors decrease both with an increase in calibration interval and with an increase in lead times is much influenced by the model chosen. Overall, the simple (0,2,1) ARIMA model does best. But the difference with a linear extrapolation is not great. The higher power polynomials are all very poor except for Oscilloquartz #51 where we have strong indication that a third power model is best for long-lead times.

An example of the simplest possible oscillator included in the project is a watch crystal (\$10 per unit), identified as Quartzmatic #1 (table 19). The factor of over 1000 by which this oscillator performs worse than any of the others is partially explained by the fact that there is no temperature control or compensation. This example is also interesting for the degree to which the higher power extrapolations degenerate for short calibration intervals. The signal-to-noise ratio is too poor to allow any but the simplest predictions for such short calibrations.

#### CONCLUSIONS

From the data presented, it is concluded that very simple prediction methods will suffice in maintaining a timing system during interruptions of the linkage with a timing reference. Clocks comparable in quality with the

Oscilloquartz units or the DTFO allow accuracies of about 1 microsecond over a day to a few tens of microseconds over more than 30 days free-running after calibration intervals as short as 1 or 2 weeks. The importance of providing an excellent operational environment for such "flywheel" oscillators must be stressed. This means, among other things, the avoidance of physical frequency adjustments, i.e., the control must be exercised with an external phase stepper or in the form of corrections which the local control processor has to apply arithmetically to all measurements.

Table 1. DEVICES EVALUATED

EVALUATION INTERVAL  
(Modified Julian Day Numbers)

## I. QUARTZ CRYSTALS

|                                       |       |               |
|---------------------------------------|-------|---------------|
| 1. OSCILLOQUARTZ 51                   | 1 pps | 44353 - 44490 |
| 2. OSCILLOQUARTZ 52                   | 1 pps | 44352 - 44496 |
| 3. URQ 10                             | 1 pps | 44236 - 44359 |
| 4. DISCIPLINED TIME<br>FREQUENCY OSC. | 1 pps | 43900 - 44280 |
| 5. AUSTRON 1220-9714                  | 5 MHz | 44160 - 44420 |

## II. RUBIDIUMS

|                        |       |               |
|------------------------|-------|---------------|
| 1. EFRATOM FRT         | 1 pps | 43903 - 44114 |
| 2. HEWLETT-PACKARD 236 | 5 MHz | 44050 - 44350 |
| 3. HEWLETT-PACKARD 229 | 5 MHz | 44120 - 44350 |

## III. CESIUMS

|                                |       |               |  |
|--------------------------------|-------|---------------|--|
| A. HEWLETT-PACKARD (HP)        |       |               |  |
| 1. HP/5060 207                 | 5 MHz | 44120 - 44330 |  |
| 2. HP/5061 1114                | 5 MHz | 44236 - 44420 |  |
| 3. HP/5061/2 <sup>1</sup> 875  | 5 MHz | 44236 - 44391 |  |
| 4. HP/5061 549                 | 5 MHz | 44120 - 44330 |  |
| 5. HP/5061/2 <sup>1</sup> 1264 | 5 MHz | 44120 - 44350 |  |

|                                |       |               |  |
|--------------------------------|-------|---------------|--|
| B. FREQUENCY TIME SYSTEM (FTS) |       |               |  |
| 1. FTS/4050 107                | 5 MHz | 44297 - 44429 |  |
| 2. FTS/4050 108                | 5 MHz | 44305 - 44429 |  |

|                            |       |               |  |
|----------------------------|-------|---------------|--|
| C. OSCILLOQUARTZ CO. (OSQ) |       |               |  |
| OSQ 68                     | 5 MHz | 44120 - 44350 |  |

|                                    |       |               |
|------------------------------------|-------|---------------|
| IV. HYDROGEN MASER 10 <sup>2</sup> | 5 MHz | 43970 - 44028 |
|------------------------------------|-------|---------------|

|                                |       |               |
|--------------------------------|-------|---------------|
| V. QUARTZMATIC #1 <sup>3</sup> | 1 pps | 43730 - 44040 |
|--------------------------------|-------|---------------|

<sup>1</sup>High performance option.<sup>2</sup>Due to lack of data, calibration intervals greater than 28 days were not computed.<sup>3</sup>As this device is for comparison purposes only, the first order solution was not computed.

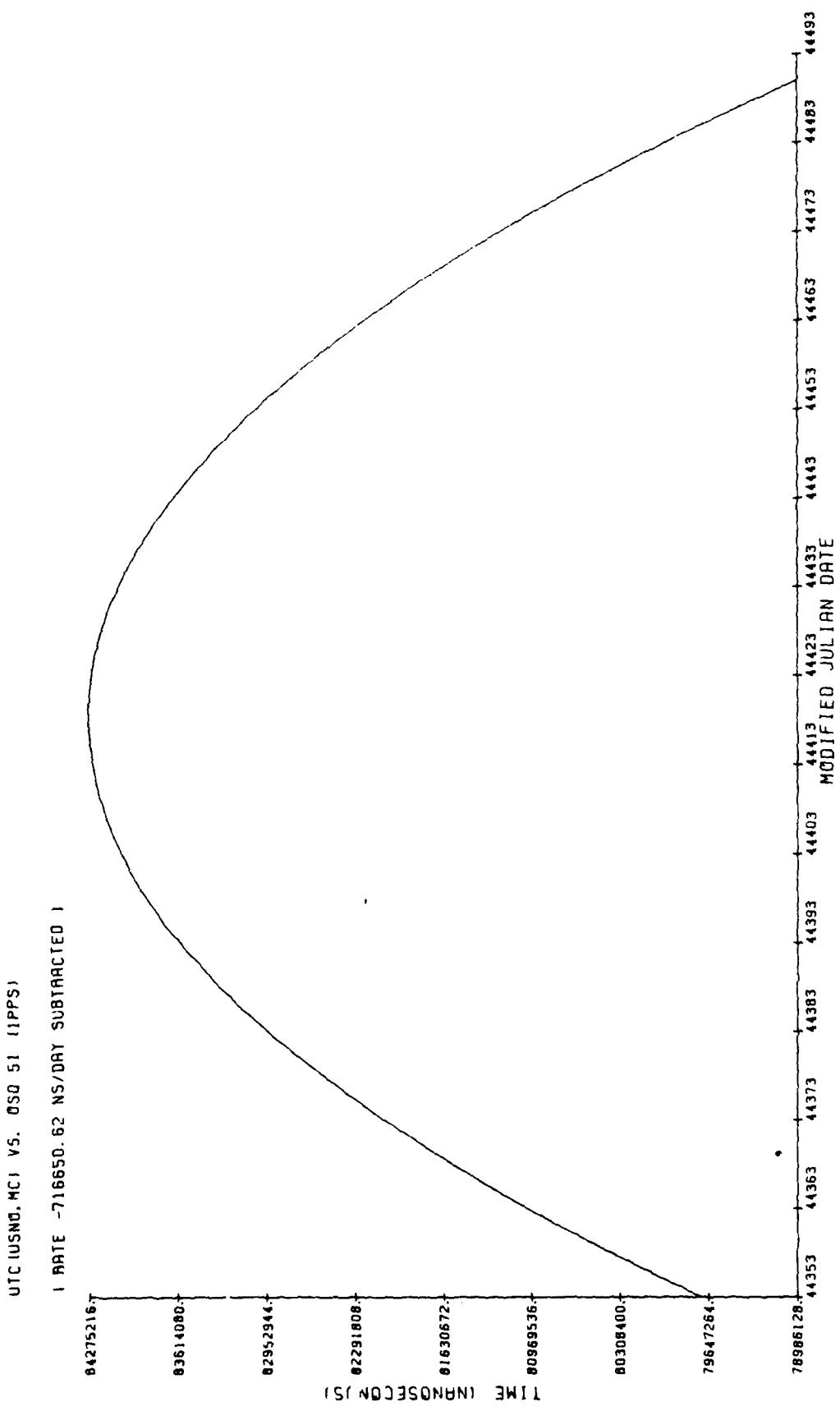


Figure 1. UTC (USNO, MC) Minus UTC (Oscillioquartz Crystal frequency oscillator 51)

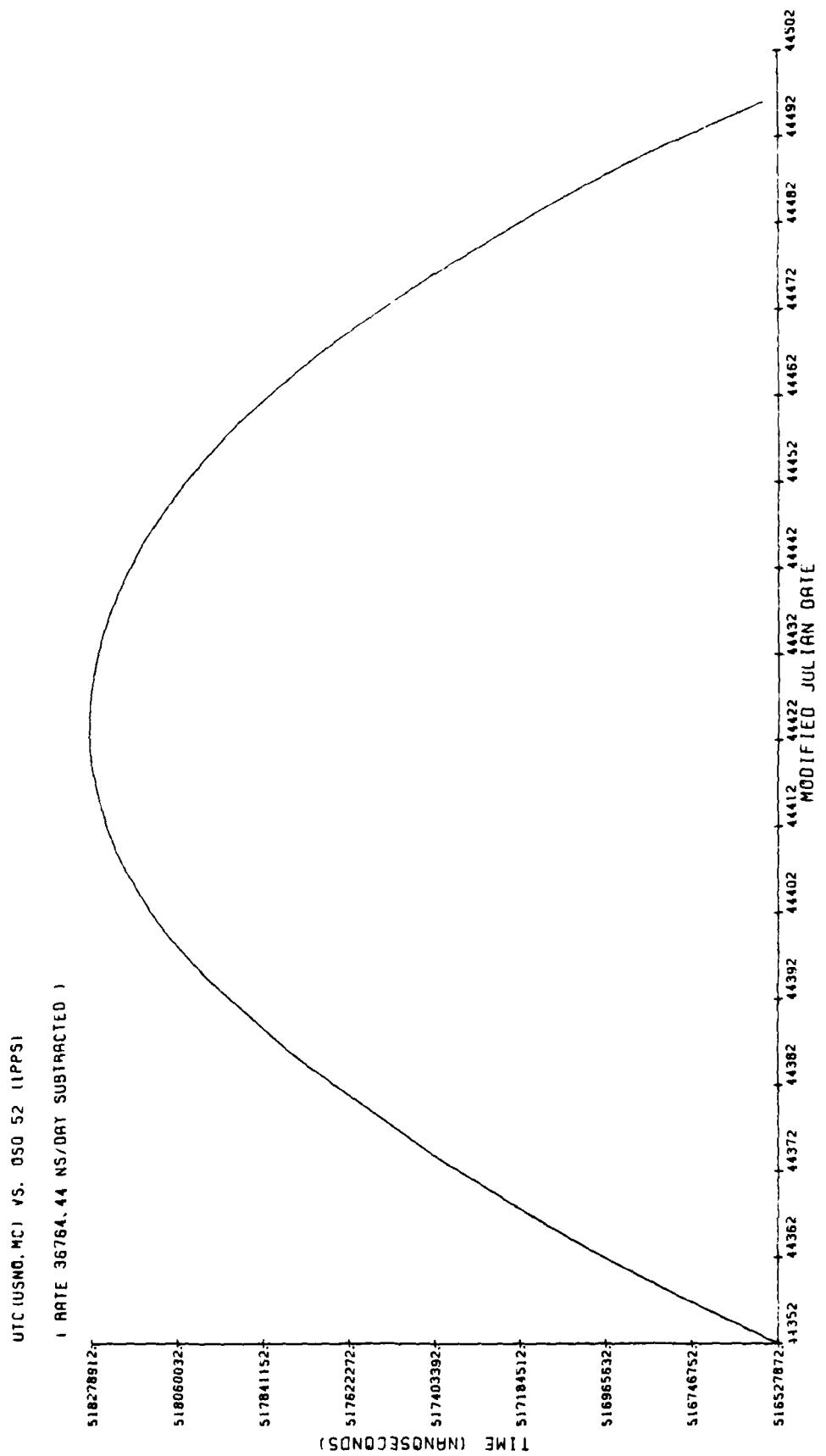


Figure 2. UTC (USNO, MC) Minus UTC (Oscillatoquartz Crystal Frequency Oscillator 52)

UTC (USNO, MC) VS. URG 10

! RATE 1392109.00 NS/DAY SUBTRACTED !

31109792.7

30706304.7

30222916.7

TIME (NANOSECONDS)

29739568.7

8

29256160.7

28777272.7

28289344.7

27805936.7

27322228.7

44286 44276 44266 44256 44246 44236 44226 UTC (USNO, MC) MINUS UTC (URG CRYSTAL FREQUENCY OSCILLATOR 10)  
MODIFIED JULIAN DATE

44316 44326 44336 44346 44356 44366

Figure 3. UTC (USNO, MC) Minus UTC (URG Crystal Frequency Oscillator 10)

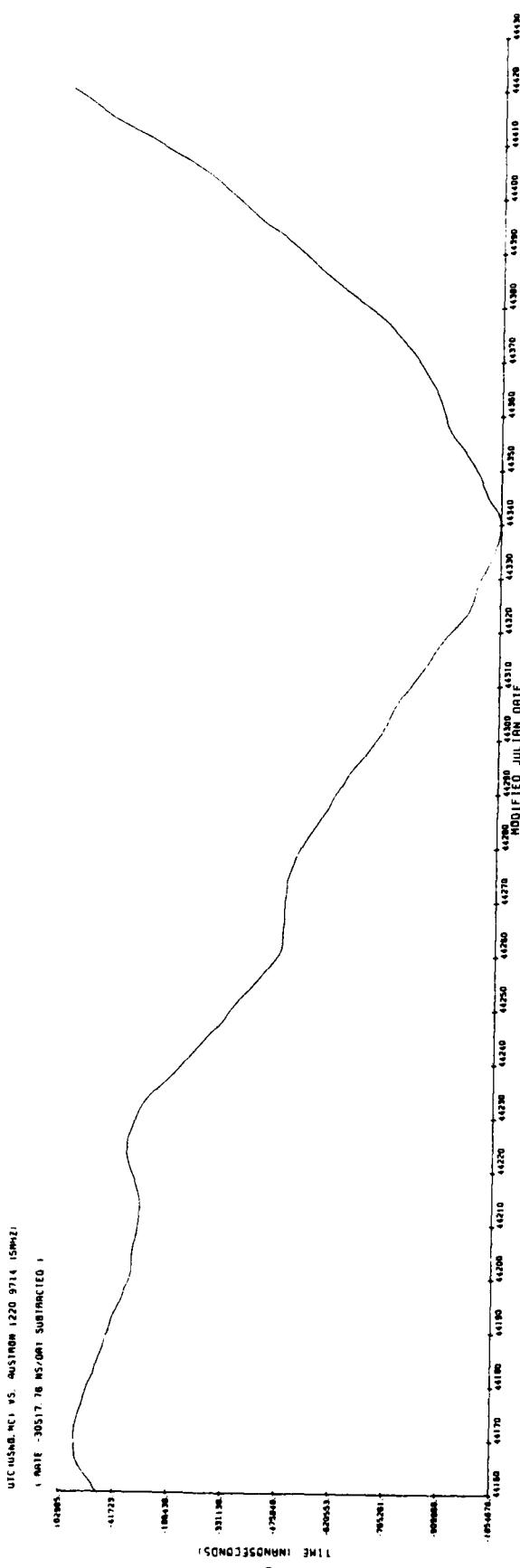


Figure 4. UTC (USNO, MC) Minus UTC (Astron Crystal) Frequency Oscillator 9714)

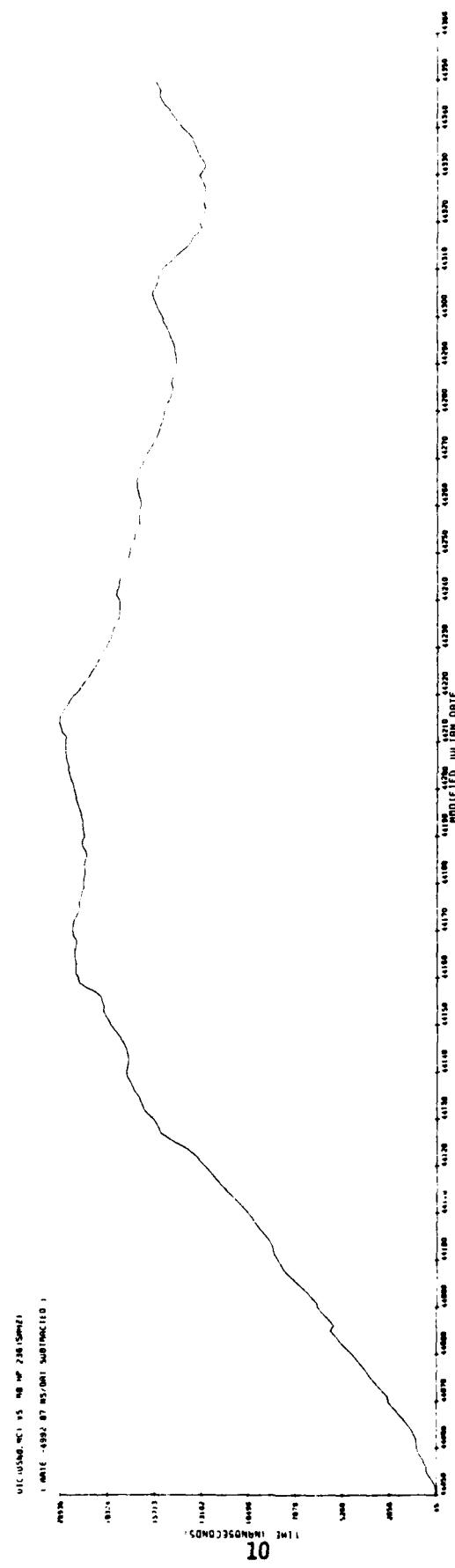


Figure 5. UTC (USNO, MC) Minus UTC (Hewlett-Packard Rubidium Frequency Oscillator 236)

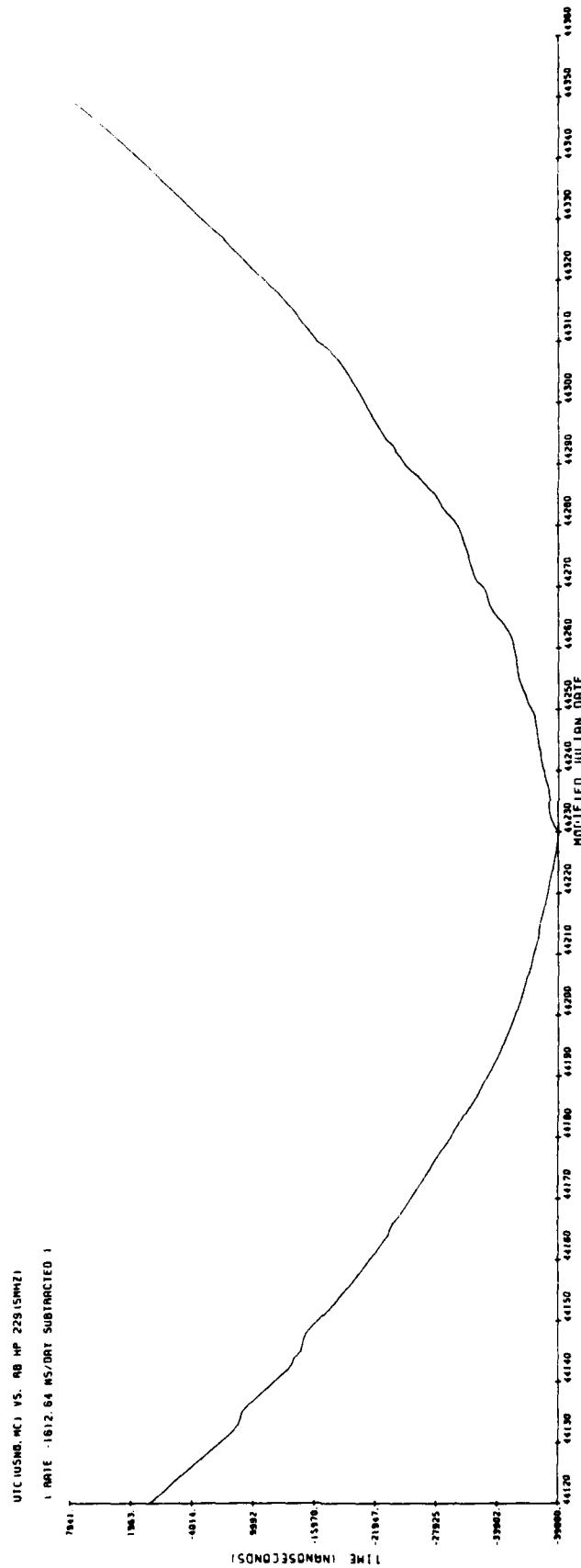


Figure 6. UTC (USNO, MC) Minus UTC (Hewlett-Packard Rubidium Frequency Oscillator 229)

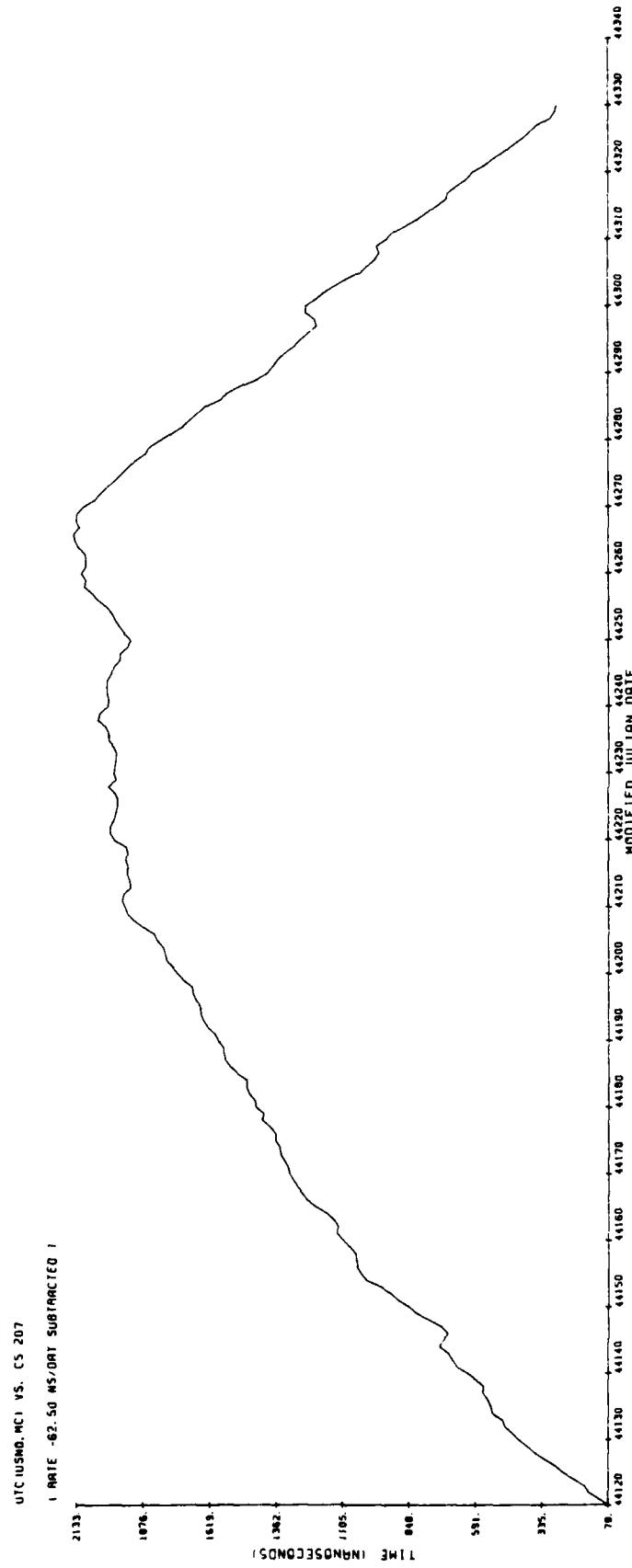


Figure 7. UTC (USNO, MC) Minus UTC (Hewlett-Packard Cesium Frequency Oscillator 207)

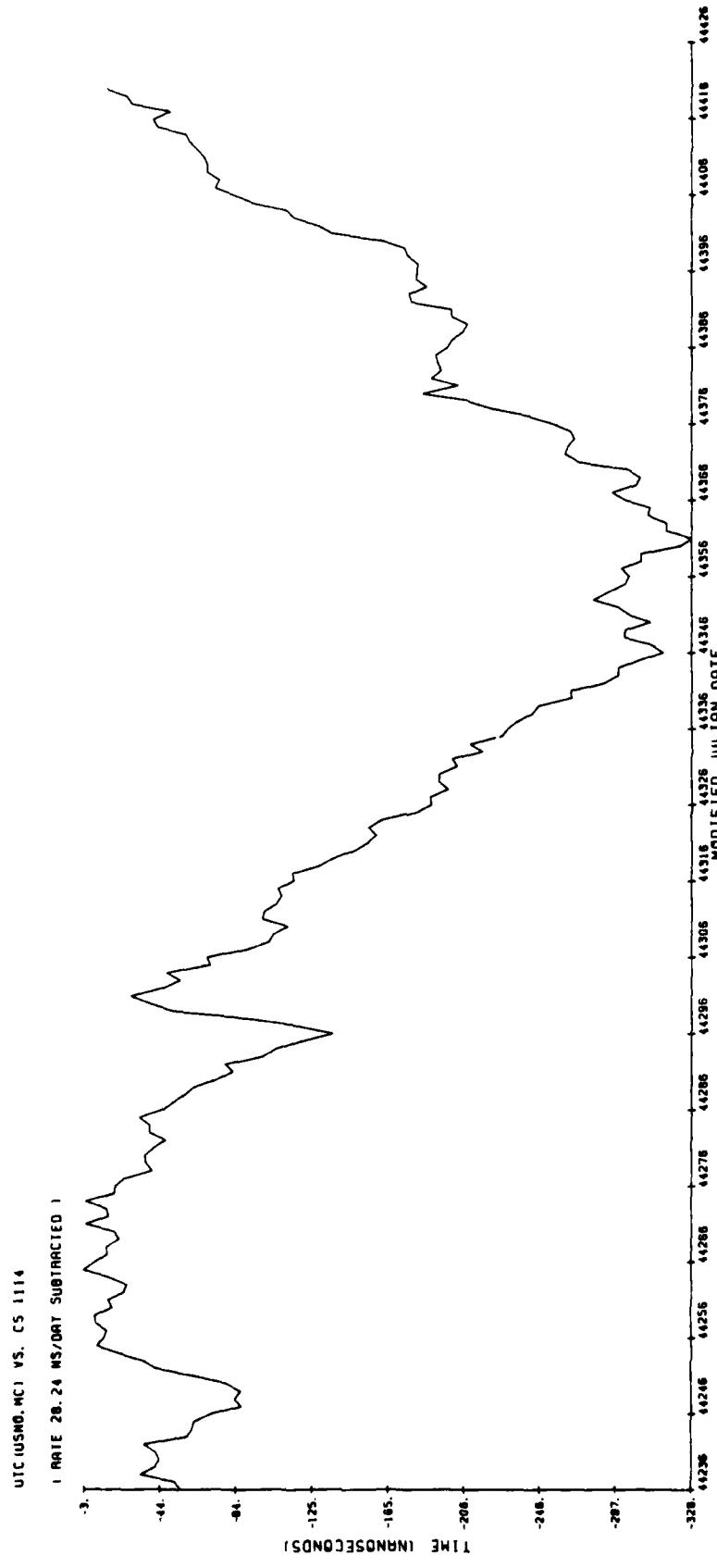


Figure 8. UTC (USNO, MC) Minus UTC (Hewlett-Packard Cesium Frequency Oscillator 1114)

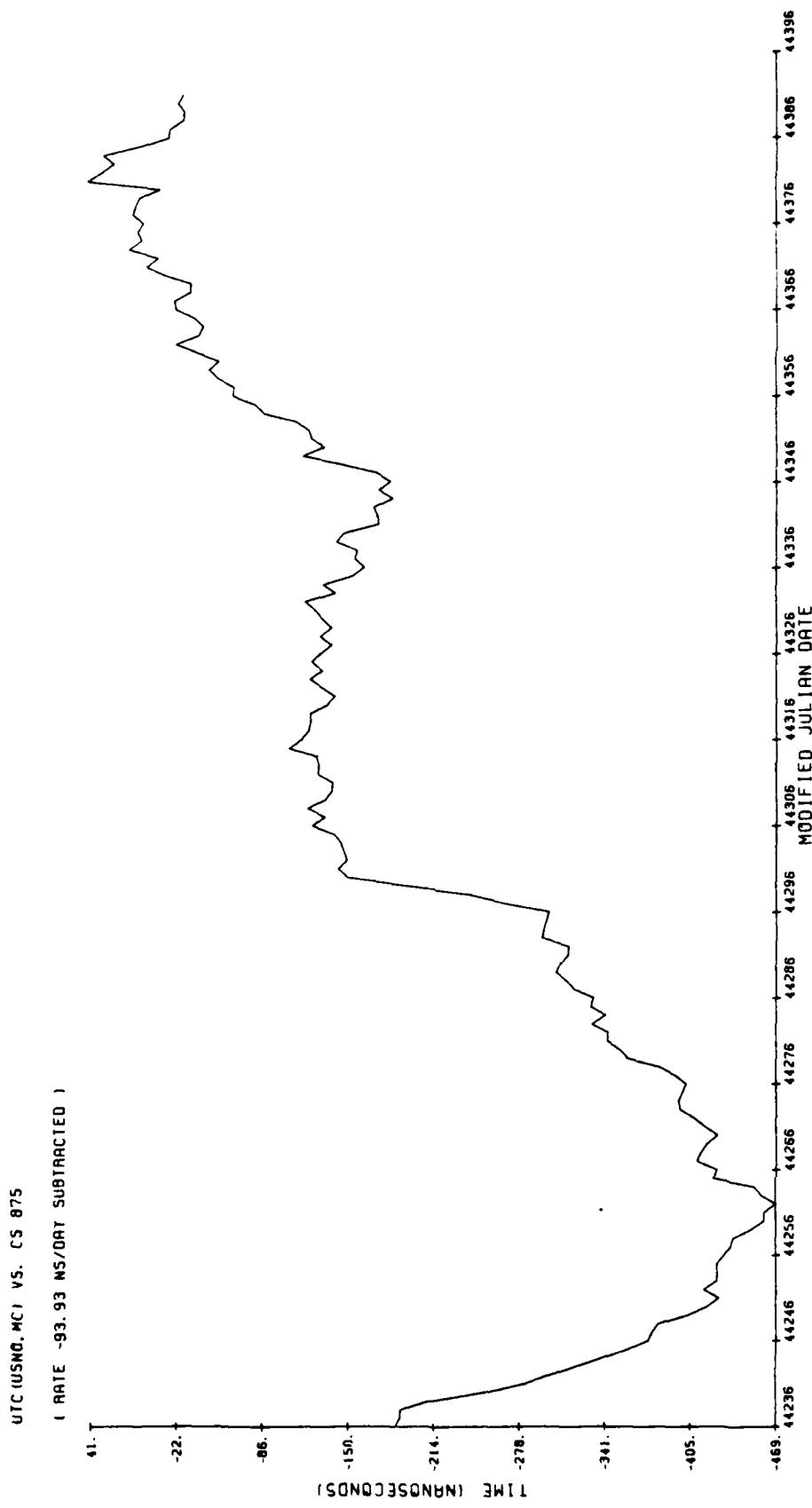


Figure 9. UTC (USNO, MC) Minus UTC (Hewlett-Packard Cesium Frequency Oscillator 875)

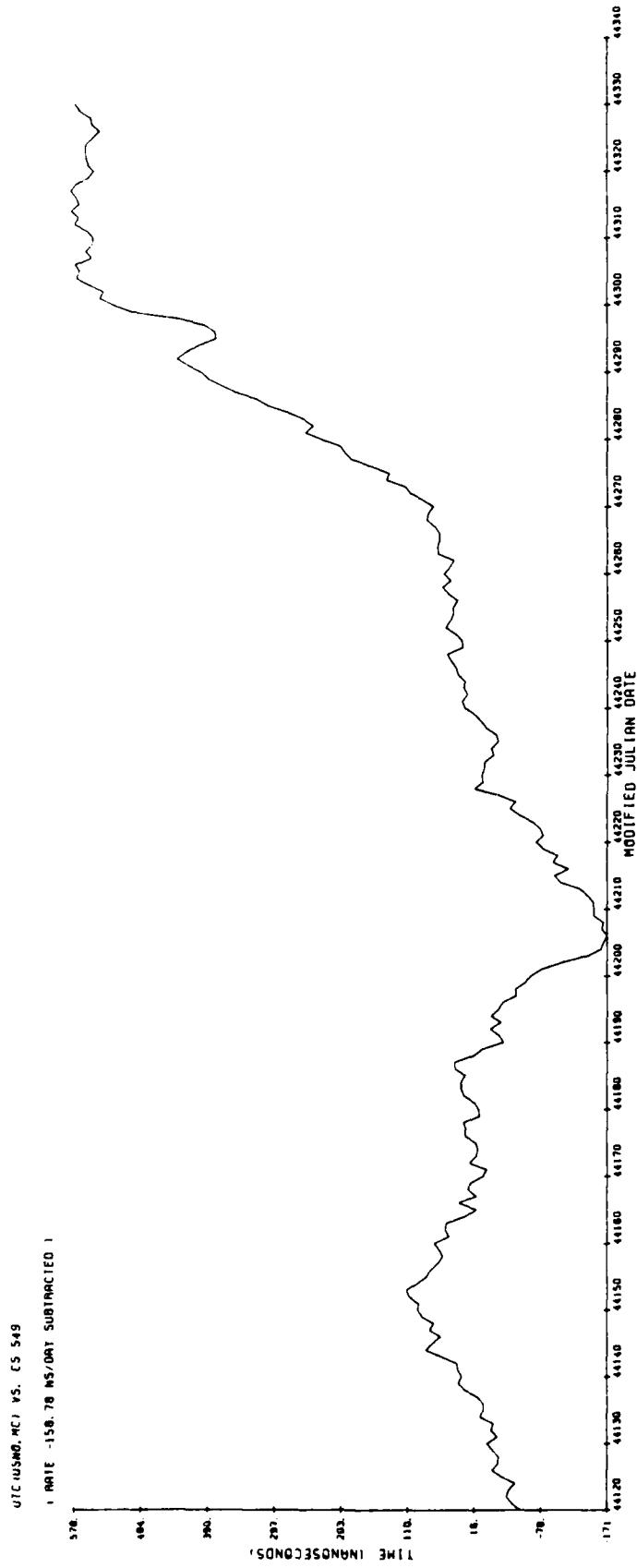


Figure 10. UTC (USNO, MC) (Hewlett-Packard Cesium Frequency Oscillator 549)

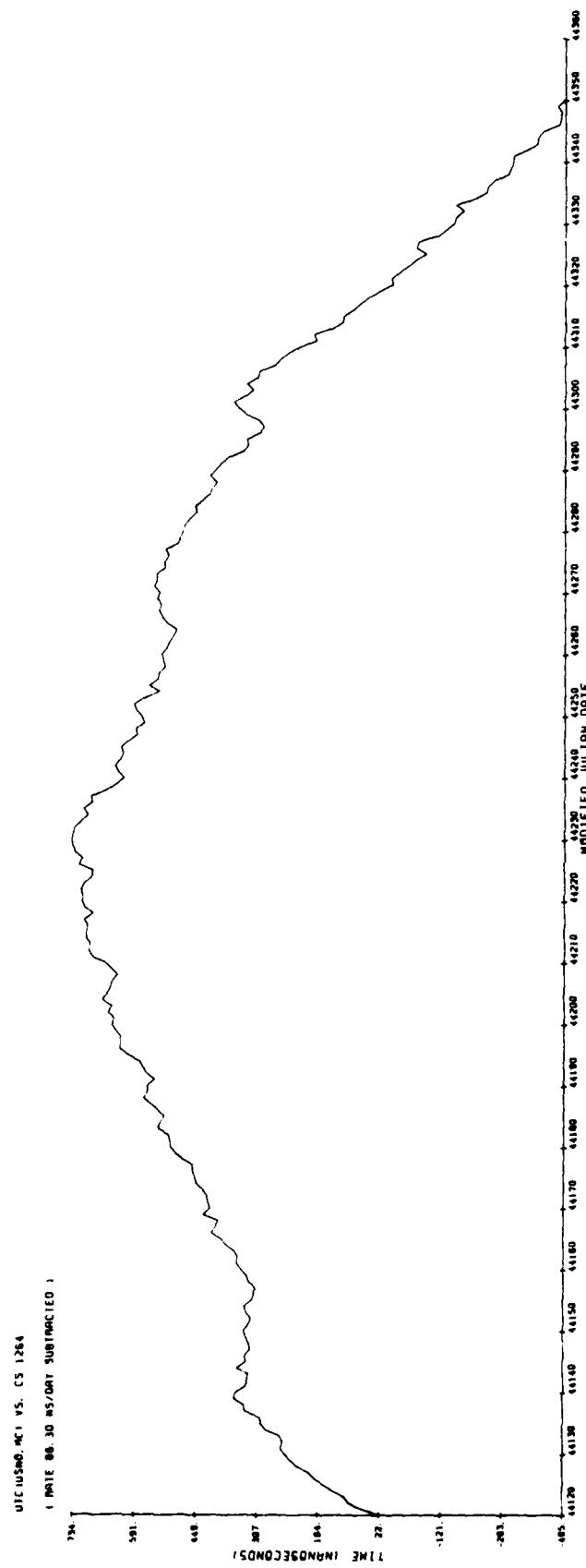


Figure 11. UTC (USNO, MC) Minus UTC (Hewlett-Packard Cesium Frequency Oscillator 1264)

UTC (USNO, MC) VS. FTS 4050-107

( RATE -148.50 NS/DAY SUBTRACTED )

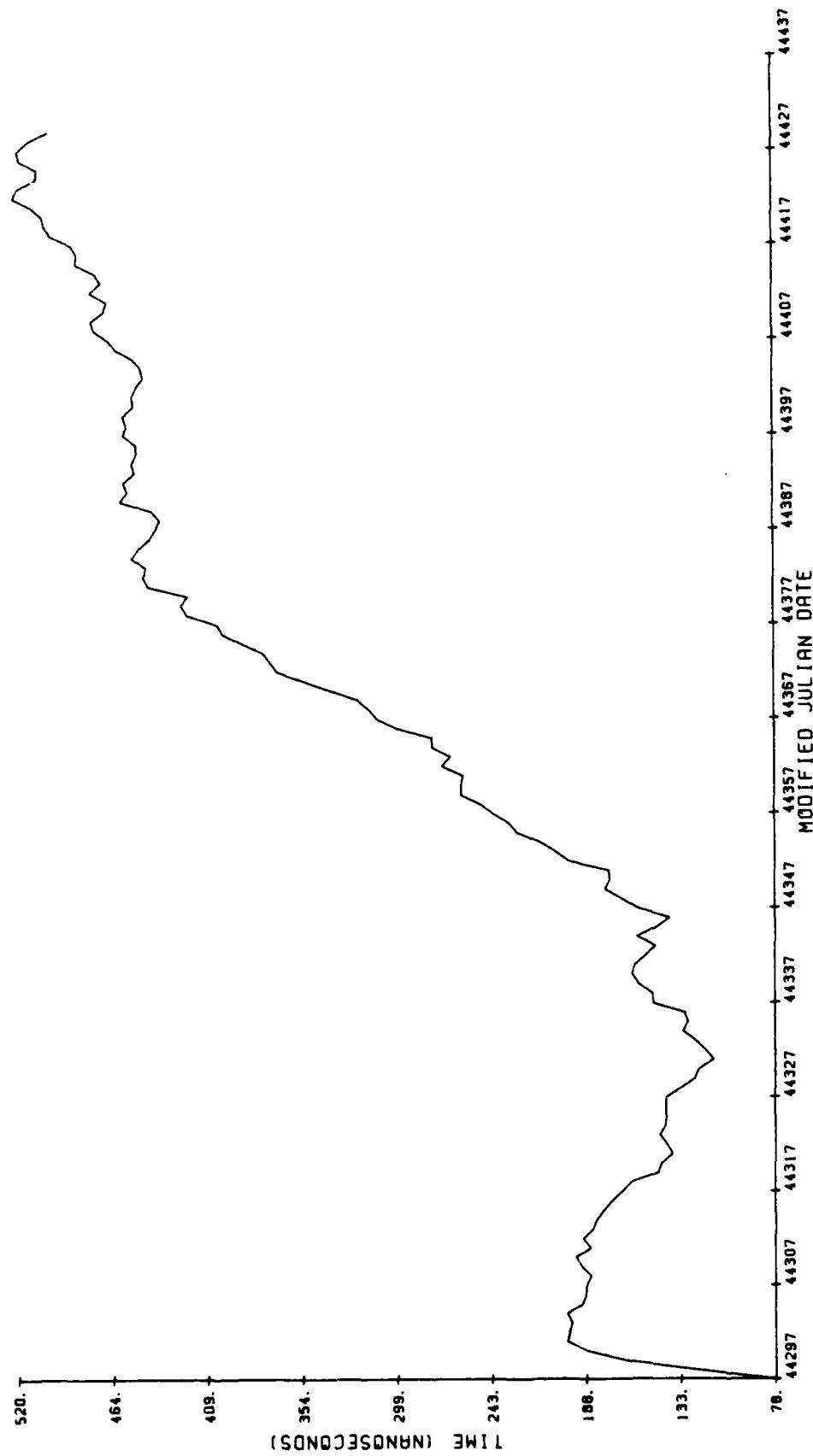
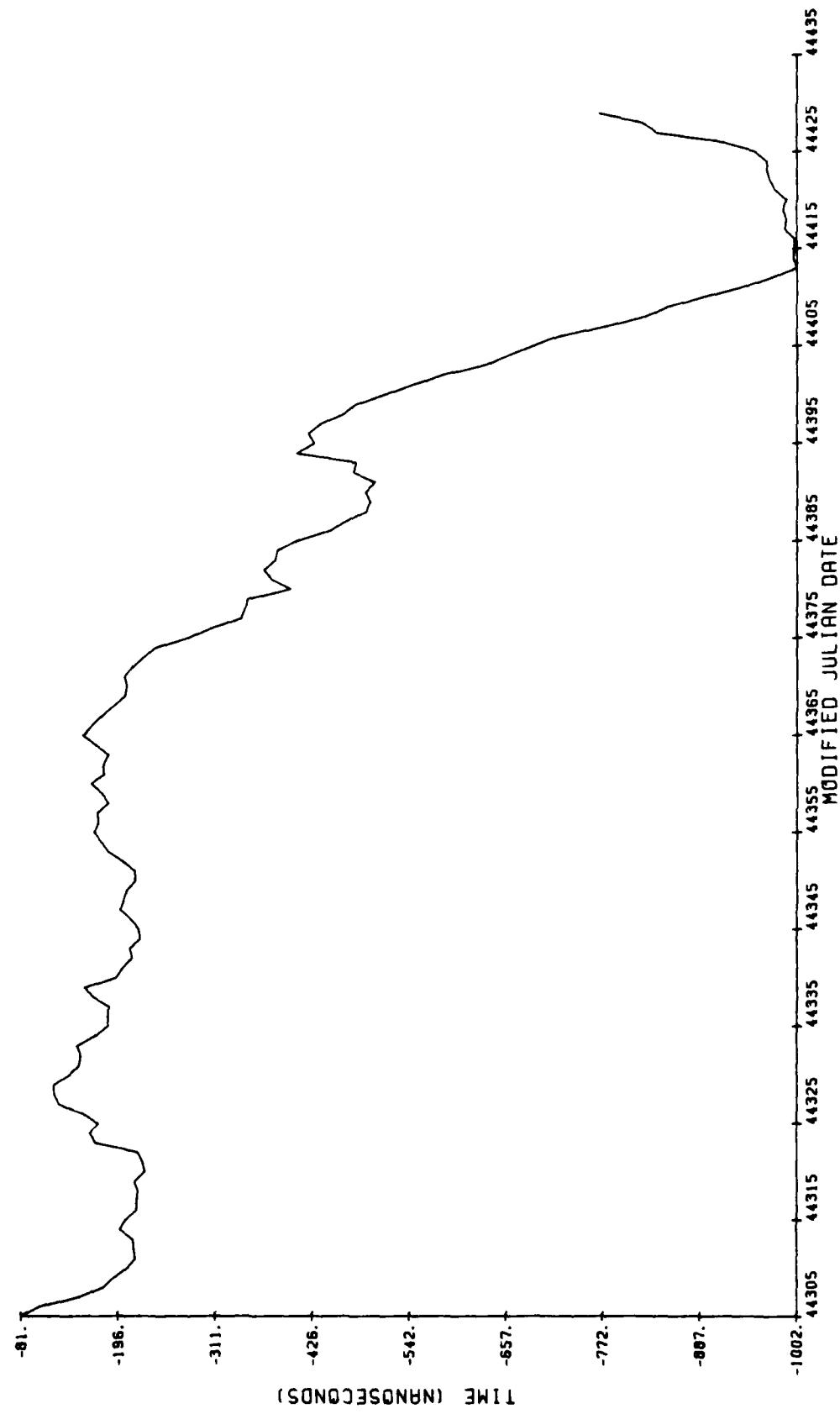


Figure 12. UTC (USNO, MC) Minus UTC (Frequency Time System Frequency Oscillator 107)

UTC (USNO, MC) VS. FTS 4050-108

1 RATE 172.82 NS/DAY SUBTRACTED )



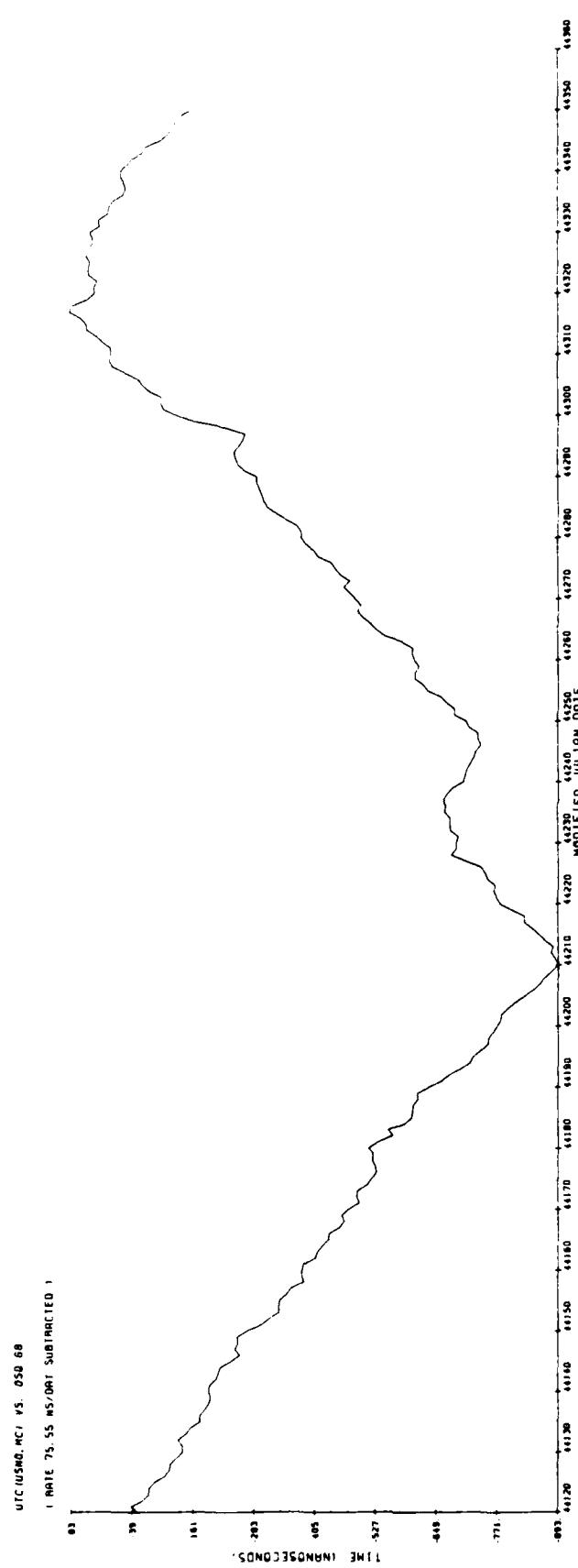


Figure 14. UTC (USNO, MC) Minus UTC (Oscillioquartz Cesium Frequency Oscillator 68)

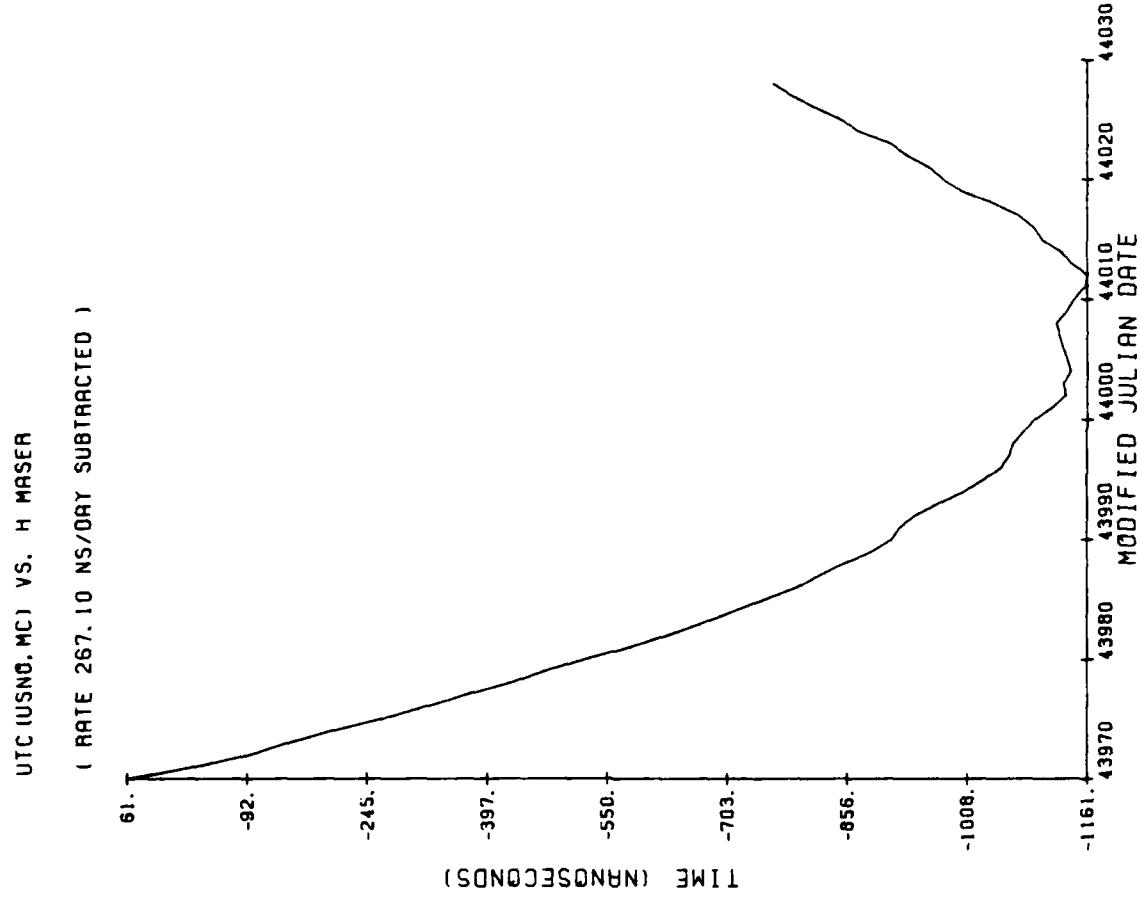


Figure 15. UTC (USNO, MC) Minus UTC (Hydrogen Maser 10)

TABLE 2  
RMS PREDICTION ERRORS  
FOR  
OSCILLOQUARTZ CRYSTAL FREQUENCY OSCILLATOR #51  
(1 pps)  
MODIFIED JULIAN DAY: 4+353 - 44470

| PREDICTION<br>LEAD TIME | ARIMA | CALIBRATION INTERVAL<br>7 DAYS |               |               |               | CALIBRATION INTERVAL<br>14 DAYS |               |               |               |
|-------------------------|-------|--------------------------------|---------------|---------------|---------------|---------------------------------|---------------|---------------|---------------|
|                         |       | 1ST<br>DEGREE                  | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE |
| 1 DAY                   | 1.5   | 12.3                           | 2.2           | 2.3           | 3.4           | 1.4                             | +2.0          | 1.9           | 3.0           |
| 2 DAYS                  | 3.5   | 22.4                           | 4.0           | 6.2           | 12.4          | 2.2                             | 59.0          | 3.3           | 5.9           |
| 5 DAYS                  | 10.0  | 53.7                           | 13.9          | 32.0          | 116.6         | 5.3                             | 121.3         | 6.0           | 17.5          |
| 10 DAYS                 | 27.7  | 173.2                          | 35.0          | 151.3         | 917.6         | 12.4                            | 268.8         | 13.0          | 56.0          |
| 15 DAYS                 | 54.9  | 325.5                          | 67.2          | 417.7         | 3570.8        | 23.5                            | 467.1         | 24.3          | 130.2         |
| 20 DAYS                 | 91.2  | 551.0                          | 115.1         | 897.7         | 9712.0        | 36.8                            | 718.1         | 39.3          | 253.5         |
| 25 DAYS                 | 133.3 | 814.1                          | 172.7         | 1648.9        | 21734.0       | 54.2                            | 1022.1        | 58.2          | 432.4         |
| 30 DAYS                 | 200.5 | 1140.1                         | 255.4         | 2333.4        | 44454.5       | 74.4                            | 1377.5        | 90.5          | 676.0         |

| PREDICTION<br>LEAD TIME | ARIMA | CALIBRATION INTERVAL<br>21 DAYS |               |               |               | CALIBRATION INTERVAL<br>28 DAYS |               |               |               |
|-------------------------|-------|---------------------------------|---------------|---------------|---------------|---------------------------------|---------------|---------------|---------------|
|                         |       | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE |
| 1 DAY                   | 1.1   | 85.7                            | 2.0           | 2.4           | 2.4           | 1.1                             | 152.6         | 2.5           | 2.5           |
| 2 DAYS                  | 2.1   | 110.6                           | 2.7           | 3.3           | 5.2           | 2.2                             | 183.9         | 3.3           | 3.9           |
| 5 DAYS                  | 5.4   | 195.2                           | 5.3           | 3.0           | 19.8          | 5.4                             | 291.8         | 5.0           | 6.4           |
| 10 DAYS                 | 11.2  | 379.1                           | 4.5           | 20.9          | 79.7          | 16.0                            | 514.7         | 13.8          | 15.3          |
| 15 DAYS                 | 20.8  | 613.9                           | 17.6          | 45.8          | 223.0         | 26.3                            | 789.1         | 23.3          | 32.0          |
| 20 DAYS                 | 33.9  | 903.5                           | 23.2          | 87.4          | 499.4         | 39.6                            | 1116.7        | 34.5          | 55.7          |
| 25 DAYS                 | 50.0  | 1247.2                          | 44.3          | 153.3         | 1019.7        | 52.5                            | 1495.0        | 46.0          | 91.9          |
| 30 DAYS                 | 67.0  | 1644.1                          | 57.1          | 241.2         | 1825.7        | 71.4                            | 1929.4        | 60.4          | 142.4         |

| PREDICTION<br>LEAD TIME | ARIMA | CALIBRATION INTERVAL<br>42 DAYS |               |               |               | CALIBRATION INTERVAL<br>56 DAYS |               |               |               |
|-------------------------|-------|---------------------------------|---------------|---------------|---------------|---------------------------------|---------------|---------------|---------------|
|                         |       | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE |
| 1 DAY                   | 1.2   | 331.9                           | 4.9           | 2.6           | 1.7           | 0.6                             | 571.7         | 4.8           | 2.0           |
| 2 DAYS                  | 1.3   | 373.5                           | 6.3           | 3.5           | 2.6           | 1.3                             | 631.5         | 6.1           | 3.4           |
| 5 DAYS                  | 2.8   | 530.0                           | 7.4           | 5.3           | 6.0           | 3.3                             | 823.3         | 9.6           | 4.2           |
| 10 DAYS                 | 7.0   | 824.3                           | 13.7          | 16.8          | 19.0          | 6.7                             | 1184.9        | 14.9          | 5.1           |
| 15 DAYS                 | 13.5  | 1167.3                          | 13.0          | 31.1          | 45.4          | 13.2                            | 1598.2        | 21.7          | 11.6          |
| 20 DAYS                 | 21.2  | 1567.0                          | 24.7          | 50.1          | 38.3          | 20.5                            | 2054.3        | 29.3          | 20.4          |
| 25 DAYS                 | 30.5  | 2019.7                          | 32.9          | 78.6          | 151.4         | 29.6                            | 2534.7        | 41.8          | 21.7          |
| 30 DAYS                 | 42.7  | 2520.2                          | 41.4          | 112.3         | 250.7         | 46.6                            | 3156.9        | 64.6          | 236.1         |

NOTE: THE RMS PREDICTION ERRORS ARE IN UNITS OF MICROSECONDS.

#### NUMBER OF SAMPLE INTERVALS

| PREDICTION<br>LEAD TIME | 7  | 14 | CALIBRATION INTERVAL |    |    |    |   |
|-------------------------|----|----|----------------------|----|----|----|---|
|                         |    |    | 21                   | 28 | 42 | 56 |   |
| DAY                     | 1  | 70 | 36                   | 24 | 15 | 12 | 8 |
|                         | 2  | 73 | 36                   | 24 | 15 | 12 | 8 |
|                         | 5  | 76 | 36                   | 24 | 15 | 12 | 8 |
|                         | 10 | 75 | 34                   | 24 | 15 | 12 | 7 |
|                         | 15 | 72 | 33                   | 22 | 15 | 12 | 7 |
|                         | 20 | 67 | 31                   | 21 | 15 | 12 | 7 |
|                         | 25 | 67 | 30                   | 18 | 15 | 11 | 6 |
|                         | 30 | 60 | 30                   | 17 | 14 | 11 | 7 |

TABLE 3  
RMS PREDICTION ERRORS  
FOR  
OSCILLOQUARTZ CRYSTAL FREQUENCY OSCILLATOR 652  
(1 pps)  
MODIFIED JULIAN DAY: 44352 - 44476

| PREDICTION<br>LEAD TIME | CALIBRATION INTERVAL<br>7 DAYS |            |            |            |            | CALIBRATION INTERVAL<br>14 DAYS |            |            |            |            |
|-------------------------|--------------------------------|------------|------------|------------|------------|---------------------------------|------------|------------|------------|------------|
|                         | ARIMA                          | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
| 1 DAY                   | 0.7                            | 4.1        | 1.5        | 1.7        | 1.8        | 0.8                             | 13.2       | 2.0        | 2.3        | 2.9        |
| 2 DAYS                  | 2.0                            | 7.3        | 2.3        | 4.3        | 5.6        | 1.2                             | 18.6       | 3.1        | 4.7        | 5.7        |
| 5 DAYS                  | 7.7                            | 20.0       | 9.2        | 23.2       | 54.5       | 5.9                             | 38.6       | 6.1        | 17.8       | 32.9       |
| 10 DAYS                 | 22.0                           | 55.3       | 20.4       | 105.3      | 511.3      | 13.5                            | 85.9       | 17.8       | 59.7       | 197.7      |
| 15 DAYS                 | 41.2                           | 105.7      | 44.0       | 284.7      | 2043.3     | 27.7                            | 152.3      | 34.8       | 138.0      | 512.1      |
| 20 DAYS                 | 71.3                           | 174.2      | 63.5       | 524.3      | 5573.7     | 40.3                            | 234.2      | 55.4       | 273.9      | 1252.3     |
| 25 DAYS                 | 105.3                          | 259.2      | 125.4      | 1135.3     | 12493.8    | 60.7                            | 333.1      | 81.7       | 466.8      | 2966.5     |
| 30 DAYS                 | 157.5                          | 360.3      | 181.0      | 1893.2     | 24424.2    | 53.9                            | 450.2      | 111.0      | 731.8      | 4573.1     |

| PREDICTION<br>LEAD TIME | CALIBRATION INTERVAL<br>21 DAYS |            |            |            |            | CALIBRATION INTERVAL<br>28 DAYS |            |            |            |            |
|-------------------------|---------------------------------|------------|------------|------------|------------|---------------------------------|------------|------------|------------|------------|
|                         | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
| 1 DAY                   | 0.3                             | 23.7       | 2.2        | 2.0        | 2.9        | 0.8                             | 48.3       | 3.0        | 2.5        | 2.2        |
| 2 DAYS                  | 1.9                             | 35.9       | 2.9        | 3.3        | 5.0        | 1.5                             | 58.1       | 4.1        | 3.6        | 3.3        |
| 5 DAYS                  | 5.5                             | 84.2       | 6.7        | 6.7        | 23.0       | 5.2                             | 92.3       | 7.7        | 9.3        | 11.7       |
| 10 DAYS                 | 15.3                            | 121.5      | 13.2       | 21.0       | 88.7       | 11.0                            | 152.4      | 15.8       | 22.8       | 40.1       |
| 15 DAYS                 | 20.1                            | 195.0      | 24.9       | 45.9       | 234.9      | 16.6                            | 248.1      | 27.4       | 39.5       | 98.0       |
| 20 DAYS                 | 34.7                            | 283.2      | 40.6       | 89.1       | 509.1      | 24.1                            | 350.7      | 41.0       | 70.0       | 184.9      |
| 25 DAYS                 | 52.1                            | 397.5      | 57.3       | 150.2      | 958.4      | 36.7                            | 469.9      | 60.0       | 112.8      | 343.2      |
| 30 DAYS                 | 74.7                            | 523.2      | 83.3       | 237.3      | 1675.4     | 51.6                            | 609.2      | 81.4       | 166.4      | 570.3      |

| PREDICTION<br>LEAD TIME | CALIBRATION INTERVAL<br>42 DAYS |            |            |            |            | CALIBRATION INTERVAL<br>56 DAYS |            |            |            |            |
|-------------------------|---------------------------------|------------|------------|------------|------------|---------------------------------|------------|------------|------------|------------|
|                         | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
| 1 DAY                   | 0.7                             | 105.6      | 5.3        | 2.6        | 2.7        | 0.6                             | 131.0      | 7.0        | 4.8        | 1.6        |
| 2 DAYS                  | 1.0                             | 120.7      | 7.1        | 3.9        | 4.1        | 1.1                             | 200.6      | 8.2        | 5.7        | 3.1        |
| 5 DAYS                  | 5.7                             | 170.5      | 11.4       | 13.7       | 12.1       | 4.9                             | 251.6      | 12.3       | 10.7       | 9.0        |
| 10 DAYS                 | 12.2                            | 261.5      | 17.2       | 21.3       | 28.1       | 13.5                            | 379.3      | 19.9       | 23.4       | 27.4       |
| 15 DAYS                 | 15.5                            | 375.0      | 30.3       | 41.8       | 59.4       | 11.0                            | 508.3      | 25.7       | 40.9       | 24.0       |
| 20 DAYS                 | 23.4                            | 503.1      | 41.3       | 71.5       | 109.3      | 14.7                            | 657.6      | 31.0       | 76.7       | 45.4       |
| 25 DAYS                 | 31.2                            | 545.7      | 53.1       | 111.3      | 133.1      | 17.7                            | 826.8      | 36.9       | 116.6      | 72.0       |
| 30 DAYS                 | 37.9                            | 805.9      | 6.0        | 163.2      | 286.5      | 25.3                            | 1013.0     | 46.4       | 164.4      | 193.9      |

NOTE: THE R'S PREDICTION ERRORS ARE IN UNITS OF MICROSECONDS.

| PREDICTION<br>LEAD TIME | NUMBER OF SAMPLE INTERVALS |    |    |    |    |    |
|-------------------------|----------------------------|----|----|----|----|----|
|                         | 7                          | 14 | 21 | 28 | 42 | 56 |
| DAY 1                   | 83                         | 40 | 24 | 20 | 12 | 8  |
| 2                       | 50                         | 40 | 24 | 20 | 12 | 8  |
| 5                       | 30                         | 40 | 24 | 20 | 12 | 8  |
| 10                      | 7.7                        | 37 | 27 | 17 | 11 | 8  |
| 15                      | 75                         | 39 | 27 | 14 | 11 | 7  |
| 20                      | 67                         | 36 | 23 | 11 | 11 | 7  |
| 25                      | 57                         | 35 | 23 | 17 | 11 | 7  |
| 30                      | 67                         | 35 | 22 | 17 | 11 | 7  |

TABLE 4  
 RMS PREDICTION ERRORS  
 FOR  
 JRC CRYSTAL FREQUENCY OSCILLATOR #10  
 MODIFIED JULIAN DAY: 44236 - 44359

| PREDICTION<br>LEAD TIME | CALIBRATION INTERVAL<br>7 DAYS  |            |            |            |            | CALIBRATION INTERVAL<br>14 DAYS |            |            |            |            |
|-------------------------|---------------------------------|------------|------------|------------|------------|---------------------------------|------------|------------|------------|------------|
|                         | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
| 1 DAY                   | 6                               | 13         | 9          | 9          | 13         | 8                               | 47         | 24         | 13         | 19         |
| 2 DAYS                  | 16                              | 23         | 19         | 23         | 47         | 16                              | 66         | 35         | 25         | 49         |
| 5 DAYS                  | 58                              | 34         | 54         | 128        | 415        | 48                              | 137        | 70         | 132        | 255        |
| 10 DAYS                 | 173                             | 155        | 139        | 640        | 3219       | 129                             | 260        | 143        | 531        | 1222       |
| 15 DAYS                 | 362                             | 275        | 383        | 1741       | 12461      | 248                             | 418        | 265        | 1282       | 3540       |
| 20 DAYS                 | 514                             | 473        | 627        | 3704       | 33532      | 412                             | 527        | 409        | 2529       | 7079       |
| 25 DAYS                 | 59                              | 698        | 832        | 6150       | 66427      | 647                             | 702        | 559        | 3525       | 11333      |
| 30 DAYS                 | 1133                            | 765        | 1149       | 10028      | 125747     | 903                             | 1167       | 768        | 5545       | 19442      |
| PREDICTION<br>LEAD TIME | CALIBRATION INTERVAL<br>21 DAYS |            |            |            |            | CALIBRATION INTERVAL<br>28 DAYS |            |            |            |            |
|                         | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
| 1 DAY                   | 6                               | 72         | 22         | 19         | 19         | 9                               | 109        | 45         | 28         | 23         |
| 2 DAYS                  | 17                              | 91         | 36         | 35         | 38         | 21                              | 134        | 63         | 43         | 45         |
| 5 DAYS                  | 54                              | 164        | 94         | 108        | 149        | 72                              | 210        | 115        | 99         | 163        |
| 10 DAYS                 | 166                             | 308        | 215        | 322        | 615        | 179                             | 374        | 213        | 246        | 676        |
| 15 DAYS                 | 236                             | 478        | 356        | 646        | 1737       | 295                             | 589        | 338        | 430        | 1639       |
| 20 DAYS                 | 425                             | 738        | 518        | 970        | 3726       | 409                             | 834        | 461        | 734        | 3419       |
| 25 DAYS                 | 512                             | 991        | 700        | 1543       | 7152       | 555                             | 1099       | 602        | 1161       | 5191       |
| 30 DAYS                 | 735                             | 1265       | 920        | 2297       | 12465      | 757                             | 1414       | 725        | 1575       | 5724       |
| PREDICTION<br>LEAD TIME | CALIBRATION INTERVAL<br>42 DAYS |            |            |            |            | CALIBRATION INTERVAL<br>56 DAYS |            |            |            |            |
|                         | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
| 1 DAY                   | 1                               | 212        | 41         | 40         | 39         | 11                              | 465        | 112        | 72         | 35         |
| 2 DAYS                  | 3                               | 248        | 46         | 56         | 59         | 23                              | 514        | 127        | 91         | 59         |
| 5 DAYS                  | 35                              | 350        | 92         | 136        | 149        | 72                              | 669        | 169        | 175        | 171        |
| 10 DAYS                 | 101                             | 544        | 122        | 326        | 422        | 151                             | 936        | 254        | 359        | 445        |
| 15 DAYS                 | 170                             | 733        | 246        | 625        | 656        | 231                             | 1233       | 372        | 593        | 973        |
| 20 DAYS                 | 380                             | 1204       | 511        | 1005       | 1183       | 294                             | 1579       | 481        | 859        | 1532       |
| 25 DAYS                 | 445                             | 1551       | 629        | 1422       | 2081       | 378                             | 1921       | 610        | 1195       | 2474       |
| 30 DAYS                 | 547                             | 1899       | 797        | 1956       | 3371       | 419                             | 2339       | 805        | 1522       | 3779       |

NOTE: THE RMS PREDICTION ERRORS ARE IN UNITS OF MICROSECONDS.

| PREDICTION<br>LEAD TIME | NUMBER OF SAMPLE INTERVALS |    |    |    |    |    |
|-------------------------|----------------------------|----|----|----|----|----|
|                         | 7                          | 14 | 21 | 28 | 42 | 56 |
| 2                       | 53                         | 32 | 20 | 15 | 3  | 8  |
| 5                       | 68                         | 32 | 20 | 15 | 3  | 3  |
| 10                      | 63                         | 32 | 20 | 15 | 3  | 3  |
| 15                      | 67                         | 32 | 19 | 15 | 3  | 3  |
| 20                      | 61                         | 32 | 17 | 14 | 3  | 3  |
| 25                      | 61                         | 31 | 16 | 14 | 3  | 3  |
| 30                      | 59                         | 28 | 16 | 14 | 3  | 7  |

TABLE 5  
RMS PREDICTION ERRORS  
FOR  
DISCIPLINED TIME FREQUENCY OSCILLATOR  
MODEL NO. FE150A SERIAL NO. 7522-5129  
MODIFIED JULIAN DAY: 43910 - 44230

| PREDICTION<br>LEAD TIME | ARIMA | CALIBRATION INTERVAL<br>7 DAYS  |               |               |               |       | CALIBRATION INTERVAL<br>14 DAYS |               |               |               |  |
|-------------------------|-------|---------------------------------|---------------|---------------|---------------|-------|---------------------------------|---------------|---------------|---------------|--|
|                         |       | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE | ARIMA | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE |  |
| 1 DAY                   | 2.0   | 4.0                             | 3.2           | 3.4           | 5.0           | 2.2   | 10.6                            | 5.3           | 4.2           | 4.9           |  |
| 2 DAYS                  | 3.7   | 7.7                             | 7.0           | 9.5           | 18.2          | 4.4   | 14.0                            | 8.3           | 8.3           | 12.3          |  |
| 5 DAYS                  | 19.7  | 13.2                            | 22.2          | 42.4          | 154.2         | 12.8  | 27.6                            | 19.1          | 28.5          | 53.4          |  |
| 10 DAYS                 | 59.0  | 40.2                            | 65.0          | 227.4         | 1271.8        | 36.9  | 56.1                            | 46.2          | 104.7         | 345.3         |  |
| 15 DAYS                 | 119.0 | 67.9                            | 130.5         | 520.7         | 4834.9        | 73.3  | 91.9                            | 88.8          | 258.1         | 1055.1        |  |
| 20 DAYS                 | 139.2 | 79.5                            | 215.3         | 1307.7        | 12930.2       | 124.3 | 132.2                           | 146.0         | 514.9         | 2507.1        |  |
| 25 DAYS                 | 233.7 | 135.8                           | 320.9         | 2385.2        | 28631.4       | 133.4 | 176.9                           | 212.2         | 890.0         | 5225.7        |  |
| 30 DAYS                 | 420.9 | 167.3                           | 461.1         | 3939.3        | 55334.3       | 247.7 | 229.6                           | 287.4         | 1408.6        | 9532.4        |  |
| PREDICTION<br>LEAD TIME | ARIMA | CALIBRATION INTERVAL<br>21 DAYS |               |               |               |       | CALIBRATION INTERVAL<br>28 DAYS |               |               |               |  |
|                         |       | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE | ARIMA | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE |  |
| 1 DAY                   | 2.4   | 13.7                            | 7.4           | 5.5           | 5.3           | 2.3   | 34.7                            | 10.9          | 7.7           | 7.6           |  |
| 2 DAYS                  | 5.0   | 23.4                            | 10.9          | 9.2           | 10.8          | 4.8   | 41.0                            | 14.4          | 12.4          | 14.1          |  |
| 5 DAYS                  | 15.9  | 39.2                            | 24.2          | 25.0          | 42.5          | 14.6  | 61.8                            | 28.6          | 31.1          | 46.1          |  |
| 10 DAYS                 | 42.4  | 67.6                            | 55.8          | 74.5          | 175.2         | 39.5  | 97.8                            | 60.0          | 90.4          | 152.6         |  |
| 15 DAYS                 | 77.1  | 105.4                           | 97.4          | 162.6         | 474.1         | 71.8  | 135.9                           | 98.5          | 188.5         | 403.9         |  |
| 20 DAYS                 | 125.1 | 150.2                           | 153.1         | 307.0         | 1056.5        | 108.5 | 181.6                           | 142.9         | 326.0         | 329.3         |  |
| 25 DAYS                 | 173.3 | 200.3                           | 213.3         | 505.3         | 2035.2        | 151.6 | 237.8                           | 196.5         | 513.8         | 1512.7        |  |
| 30 DAYS                 | 233.1 | 255.9                           | 285.7         | 778.2         | 3566.1        | 201.4 | 298.3                           | 258.3         | 758.7         | 2527.4        |  |
| PREDICTION<br>LEAD TIME | ARIMA | CALIBRATION INTERVAL<br>42 DAYS |               |               |               |       | CALIBRATION INTERVAL<br>56 DAYS |               |               |               |  |
|                         |       | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE | ARIMA | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE |  |
| 1 DAY                   | 2.5   | 49.3                            | 11.6          | 13.5          | 10.8          | 2.2   | 74.0                            | 25.2          | 20.7          | 14.6          |  |
| 2 DAYS                  | 5.1   | 56.0                            | 14.4          | 13.5          | 17.2          | 4.6   | 31.3                            | 29.9          | 27.6          | 20.2          |  |
| 5 DAYS                  | 13.1  | 75.2                            | 23.4          | 36.5          | 44.6          | 10.8  | 104.0                           | 45.4          | 47.8          | 37.6          |  |
| 10 DAYS                 | 33.1  | 110.5                           | 41.3          | 75.4          | 133.3         | 27.4  | 146.4                           | 74.3          | 88.5          | 57.6          |  |
| 15 DAYS                 | 53.3  | 152.6                           | 66.3          | 131.4         | 291.5         | 43.0  | 197.4                           | 105.8         | 145.4         | 175.3         |  |
| 20 DAYS                 | 92.0  | 203.7                           | 97.2          | 210.2         | 556.7         | 55.9  | 253.5                           | 143.0         | 224.4         | 322.3         |  |
| 25 DAYS                 | 127.1 | 254.1                           | 130.6         | 306.2         | 946.3         | 37.9  | 315.9                           | 182.6         | 326.7         | 519.1         |  |
| 30 DAYS                 | 163.0 | 323.5                           | 170.0         | 433.5         | 1523.7        | 114.1 | 395.5                           | 226.4         | 451.2         | 792.4         |  |

NOTE: THE RMS PREDICTION ERRORS ARE IN UNITS OF MICROSECONDS.

#### NUMBER OF SAMPLE INTERVALS

| PREDICTION<br>LEAD TIME | 7   | 14  | CALIBRATION INTERVAL |    |    | 56 |
|-------------------------|-----|-----|----------------------|----|----|----|
|                         |     |     | 21                   | 23 | 42 |    |
| 1 DAY                   | 213 | 103 | 72                   | 52 | 36 | 24 |
| 2                       | 213 | 103 | 72                   | 52 | 30 | 24 |
| 3                       | 213 | 103 | 72                   | 52 | 36 | 24 |
| 10                      | 213 | 107 | 72                   | 52 | 30 | 24 |
| 15                      | 211 | 104 | 72                   | 52 | 30 | 23 |
| 20                      | 210 | 102 | 59                   | 52 | 35 | 22 |
| 25                      | 207 | 102 | 58                   | 51 | 30 | 22 |
| 30                      | 202 | 102 | 56                   | 51 | 34 | 22 |

TABLE 6  
RMS PREDICTION ERRORS  
FOR  
AUSTROM CRYSTAL FREQUENCY OSCILLATOR MODEL 1220 #9714  
MODIFIED JULIAN DAY: 44150 - 44420

| PREDICTION | LEAD TIME | CALIBRATION INTERVAL |            |            |            | CALIBRATION INTERVAL |       |            |            |            |            |
|------------|-----------|----------------------|------------|------------|------------|----------------------|-------|------------|------------|------------|------------|
|            |           | 7 DAYS               |            | 14 DAYS    |            | 21 DAYS              |       | 28 DAYS    |            |            |            |
|            |           | ARIMA                | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE           | ARIMA | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
|            | 1 DAY     | 2                    | 6          | 3          | 3          | 4                    | 3     | 10         | 7          | 4          | 4          |
|            | 2 DAYS    | 6                    | 9          | 7          | 9          | 10                   | 6     | 14         | 11         | 3          | 11         |
|            | 5 DAYS    | 22                   | 21         | 25         | 51         | 140                  | 19    | 23         | 27         | 32         | 60         |
|            | 10 DAYS   | 68                   | 43         | 75         | 247        | 1053                 | 47    | 53         | 60         | 115        | 310        |
|            | 15 DAYS   | 137                  | 70         | 151        | 677        | 3174                 | 89    | 84         | 103        | 271        | 955        |
|            | 20 DAYS   | 233                  | 101        | 256        | 1447       | 10003                | 142   | 114        | 163        | 530        | 2236       |
|            | 25 DAYS   | 350                  | 136        | 362        | 2587       | 23293                | 209   | 147        | 245        | 905        | 4223       |
|            | 30 DAYS   | 499                  | 175        | 547        | 4291       | 45301                | 293   | 187        | 337        | 1411       | 7615       |
| <br>       |           |                      |            |            |            |                      |       |            |            |            |            |
| PREDICTION | LEAD TIME | CALIBRATION INTERVAL |            |            |            | CALIBRATION INTERVAL |       |            |            |            |            |
|            |           | 21 DAYS              |            | 28 DAYS    |            | 21 DAYS              |       | 28 DAYS    |            |            |            |
|            |           | ARIMA                | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE           | ARIMA | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
|            | 1 DAY     | 3                    | 18         | 9          | 7          | 7                    | 3     | 33         | 12         | 10         | 8          |
|            | 2 DAYS    | 7                    | 23         | 14         | 13         | 15                   | 6     | 40         | 17         | 15         | 16         |
|            | 5 DAYS    | 20                   | 38         | 29         | 33         | 61                   | 20    | 62         | 34         | 40         | 53         |
|            | 10 DAYS   | 53                   | 59         | 56         | 38         | 250                  | 47    | 98         | 74         | 109        | 180        |
|            | 15 DAYS   | 97                   | 101        | 117        | 136        | 669                  | 92    | 139        | 129        | 215        | 442        |
|            | 20 DAYS   | 161                  | 141        | 185        | 342        | 1475                 | 142   | 177        | 191        | 365        | 923        |
|            | 25 DAYS   | 242                  | 194        | 276        | 569        | 2795                 | 203   | 217        | 267        | 574        | 1639       |
|            | 30 DAYS   | 330                  | 226        | 306        | 854        | 4375                 | 272   | 267        | 354        | 937        | 2980       |
| <br>       |           |                      |            |            |            |                      |       |            |            |            |            |
| PREDICTION | LEAD TIME | CALIBRATION INTERVAL |            |            |            | CALIBRATION INTERVAL |       |            |            |            |            |
|            |           | 42 DAYS              |            | 56 DAYS    |            | 42 DAYS              |       | 56 DAYS    |            |            |            |
|            |           | ARIMA                | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE           | ARIMA | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
|            | 1 DAY     | 2                    | 49         | 24         | 11         | 9                    | 3     | 87         | 40         | 29         | 17         |
|            | 2 DAYS    | 5                    | 56         | 29         | 15         | 15                   | 5     | 95         | 47         | 38         | 24         |
|            | 5 DAYS    | 19                   | 79         | 50         | 33         | 43                   | 15    | 117        | 69         | 71         | 58         |
|            | 10 DAYS   | 54                   | 120        | 91         | 87         | 132                  | 41    | 159        | 119        | 145        | 141        |
|            | 15 DAYS   | 17                   | 165        | 130        | 169        | 291                  | 76    | 202        | 176        | 255        | 218        |
|            | 20 DAYS   | 145                  | 213        | 136        | 232        | 548                  | 113   | 245        | 236        | 400        | 529        |
|            | 25 DAYS   | 179                  | 254        | 240        | 433        | 925                  | 171   | 294        | 320        | 603        | 906        |
|            | 30 DAYS   | 259                  | 327        | 300        | 624        | 1440                 | 223   | 348        | 392        | 820        | 1415       |

NOTE: THE RMS PREDICTION ERRORS ARE IN UNITS OF MICROSECONDS.

| PREDICTION | LEAD TIME | NUMBER OF SAMPLE INTERVALS |    |    |    |    |
|------------|-----------|----------------------------|----|----|----|----|
|            |           | 7                          | 14 | 21 | 28 | 42 |
| DAY        | 1         | 143                        | 72 | 48 | 35 | 24 |
|            | 2         | 143                        | 72 | 48 | 35 | 24 |
|            | 5         | 143                        | 72 | 48 | 35 | 24 |
|            | 10        | 146                        | 72 | 48 | 35 | 23 |
|            | 15        | 144                        | 72 | 48 | 35 | 23 |
|            | 20        | 141                        | 71 | 47 | 35 | 22 |
|            | 25        | 135                        | 61 | 45 | 35 | 21 |
|            | 30        | 129                        | 60 | 45 | 35 | 21 |

TABLE 7  
 RMS PREDICTION ERRORS  
 FOR  
 EFRATOR RUBIDIUM FREQUENCY OSCILLATOR  
 TYPE FRT  
 MODIFIED JULIAN DAY: 43903 - 44114

| PREDICTION<br>LEAD TIME | ARIMA | CALIBRATION INTERVAL<br>7 DAYS  |               |               |               | CALIBRATION INTERVAL<br>14 DAYS |               |               |               |
|-------------------------|-------|---------------------------------|---------------|---------------|---------------|---------------------------------|---------------|---------------|---------------|
|                         |       | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE | 1ST<br>ARIMA                    | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE |
| 1 DAY                   | 1.4   | 1.2                             | 0.6           | 0.7           | 1.0           | 0.6                             | 2.6           | 1.9           | 1.2           |
| 2 DAYS                  | 1.2   | 1.3                             | 1.5           | 1.9           | 3.8           | 1.4                             | 3.3           | 2.8           | 3.0           |
| 5 DAYS                  | 5.1   | 3.7                             | 5.0           | 10.1          | 35.2          | 4.7                             | 5.1           | 6.2           | 10.7          |
| 10 DAYS                 | 15.4  | 7.3                             | 13.9          | 45.5          | 232.1         | 12.5                            | 8.9           | 15.0          | 39.1          |
| 15 DAYS                 | 34.9  | 10.9                            | 39.6          | 125.0         | 1038.4        | 23.2                            | 12.7          | 27.4          | 92.3          |
| 20 DAYS                 | 57.4  | 14.4                            | 65.3          | 261.2         | 2950.2        | 37.6                            | 16.1          | 43.8          | 182.6         |
| 25 DAYS                 | 87.7  | 17.5                            | 100.6         | 477.9         | 6648.0        | 54.4                            | 19.8          | 62.4          | 318.1         |
| 30 DAYS                 | 123.9 | 21.4                            | 142.4         | 797.7         | 13181.9       | 74.1                            | 24.1          | 85.5          | 504.2         |
|                         |       |                                 |               |               |               |                                 |               |               | 3389.1        |
| PREDICTION<br>LEAD TIME | ARIMA | CALIBRATION INTERVAL<br>21 DAYS |               |               |               | CALIBRATION INTERVAL<br>28 DAYS |               |               |               |
|                         |       | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE | ARIMA                           | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE |
| 1 DAY                   | 1.7   | 3.3                             | 2.7           | 1.4           | 1.3           | 0.5                             | 3.6           | 2.8           | 3.2           |
| 2 DAYS                  | 1.0   | 4.2                             | 4.2           | 2.4           | 2.9           | 1.2                             | 4.3           | 3.4           | 4.7           |
| 5 DAYS                  | 3.9   | 6.3                             | 8.2           | 6.3           | 13.4          | 3.5                             | 6.5           | 5.7           | 10.6          |
| 10 DAYS                 | 10.0  | 12.0                            | 17.5          | 19.6          | 60.5          | 8.0                             | 10.2          | 11.1          | 28.4          |
| 15 DAYS                 | 17.6  | 14.3                            | 29.4          | 42.9          | 157.6         | 13.1                            | 13.6          | 16.4          | 57.7          |
| 20 DAYS                 | 27.9  | 18.5                            | 44.4          | 83.0          | 388.4         | 20.8                            | 17.4          | 23.2          | 102.0         |
| 25 DAYS                 | 39.0  | 19.9                            | 60.7          | 137.6         | 743.5         | 29.3                            | 21.6          | 31.2          | 162.1         |
| 30 DAYS                 | 52.4  | 23.9                            | 81.4          | 213.3         | 1309.3        | 39.7                            | 39.7          | 42.4          | 250.1         |
|                         |       |                                 |               |               |               |                                 |               |               | 778.9         |
| PREDICTION<br>LEAD TIME | ARIMA | CALIBRATION INTERVAL<br>42 DAYS |               |               |               | CALIBRATION INTERVAL<br>56 DAYS |               |               |               |
|                         |       | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE | ARIMA                           | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE |
| 1 DAY                   | 1.5   | 5.0                             | 2.5           | 3.1           | 2.3           | 0.6                             | 6.5           | 3.8           | 3.1           |
| 2 DAYS                  | 1.0   | 5.5                             | 3.2           | 4.1           | 3.8           | 1.1                             | 7.0           | 4.8           | 4.0           |
| 5 DAYS                  | 2.9   | 7.3                             | 5.5           | 7.5           | 10.6          | 1.7                             | 9.1           | 8.1           | 7.2           |
| 10 DAYS                 | 5.6   | 10.1                            | 10.1          | 16.1          | 32.2          | 3.8                             | 14.2          | 14.4          | 12.7          |
| 15 DAYS                 | 11.7  | 14.7                            | 15.7          | 23.3          | 72.5          | 6.6                             | 20.4          | 20.6          | 18.2          |
| 20 DAYS                 | 15.7  | 19.5                            | 21.7          | 43.9          | 135.0         | 9.6                             | 25.9          | 27.2          | 24.2          |
| 25 DAYS                 | 19.4  | 24.4                            | 23.2          | 64.2          | 229.6         | 10.8                            | 31.4          | 32.3          | 30.8          |
| 30 DAYS                 | 24.1  | 30.7                            | 34.1          | 87.3          | 368.0         | 14.8                            | 34.4          | 41.5          | 42.3          |
|                         |       |                                 |               |               |               |                                 |               |               | 214.1         |

NOTE: THE RMS PREDICTION ERRORS ARE IN UNITS OF MICROSECONDS.

| PREDICTION<br>LEAD TIME | 7   | 14 | NUMBER OF SAMPLE INTERVALS |    |    |    |
|-------------------------|-----|----|----------------------------|----|----|----|
|                         |     |    | CALIBRATION INTERVAL       | 21 | 28 | 42 |
| DAY 1                   | 120 | 60 | 40                         | 28 | 20 | 12 |
| 2                       | 120 | 60 | 40                         | 28 | 20 | 12 |
| 5                       | 120 | 60 | 40                         | 23 | 20 | 12 |
| 10                      | 119 | 60 | 39                         | 23 | 20 | 12 |
| 15                      | 114 | 53 | 39                         | 22 | 19 | 12 |
| 20                      | 113 | 53 | 35                         | 27 | 17 | 11 |
| 25                      | 111 | 53 | 35                         | 26 | 17 | 11 |
| 30                      | 105 | 52 | 34                         | 24 | 19 | 9  |

TABLE 8  
RMS PREDICTION ERRORS  
FJP  
HP RUEIDUM FREQUE.CY OSCILLATOR #230  
MODIFIED JULIAN DAY: 44050 - 44350

| PREDICTION | LEAD TIME  | CALIBRATION INTERVAL |            |            |            |            | CALIBRATION INTERVAL |            |            |            |            | CALIBRATION INTERVAL |            |            |
|------------|------------|----------------------|------------|------------|------------|------------|----------------------|------------|------------|------------|------------|----------------------|------------|------------|
|            |            | 7 DAYS               |            | 14 DAYS    |            | 21 DAYS    | 28 DAYS              |            | 35 DAYS    |            | 42 DAYS    | 56 DAYS              |            |            |
| ARIMA      | 1ST DEGREE | 2ND DEGREE           | 3RD DEGREE | 4TH DEGREE | ARIMA      | 1ST DEGREE | 2ND DEGREE           | 3RD DEGREE | 4TH DEGREE | ARIMA      | 1ST DEGREE | 2ND DEGREE           | 3RD DEGREE | 4TH DEGREE |
| 1 DAY      | 0.1        | 0.2                  | 0.1        | 0.2        | 0.1        | 0.2        | 0.2                  | 0.2        | 0.1        | 0.1        | 0.5        | 0.3                  | 0.2        | 0.2        |
| 2 DAYS     | 0.2        | 0.2                  | 0.2        | 0.4        | 0.8        | 0.2        | 0.3                  | 0.3        | 0.3        | 0.2        | 0.6        | 0.5                  | 0.3        | 0.3        |
| 5 DAYS     | 0.6        | 0.5                  | 0.7        | 1.9        | 7.6        | 0.5        | 0.6                  | 0.7        | 1.0        | 0.6        | 1.0        | 0.9                  | 1.0        | 1.0        |
| 10 DAYS    | 1.9        | 1.1                  | 2.1        | 3.7        | 58.5       | 1.3        | 1.1                  | 1.6        | 3.3        | 1.3        | 1.6        | 1.6                  | 3.3        | 10.0       |
| 15 DAYS    | 3.7        | 1.7                  | 4.1        | 23.5       | 221.5      | 2.7        | 1.6                  | 3.1        | 7.7        | 2.7        | 1.6        | 3.1                  | 7.7        | 31.4       |
| 20 DAYS    | 6.2        | 2.3                  | 5.8        | 43.4       | 598.4      | 4.4        | 2.0                  | 4.9        | 14.9       | 4.4        | 2.0        | 4.9                  | 14.9       | 74.9       |
| 25 DAYS    | 9.4        | 2.9                  | 10.3       | 89.2       | 1323.5     | 6.4        | 2.4                  | 7.0        | 25.4       | 6.4        | 2.4        | 7.0                  | 25.4       | 154.5      |
| 30 DAYS    | 13.3       | 3.4                  | 14.5       | 142.4      | 2513.7     | 8.6        | 2.7                  | 9.4        | 40.0       | 8.6        | 2.7        | 9.4                  | 40.0       | 283.4      |
|            |            |                      |            |            |            |            |                      |            |            |            |            |                      |            |            |
| PREDICTION |            | CALIBRATION INTERVAL |            |            |            |            | CALIBRATION INTERVAL |            |            |            |            | CALIBRATION INTERVAL |            |            |
| LEAD TIME  | ARIMA      | 1ST DEGREE           | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA      | 1ST DEGREE           | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA      | 1ST DEGREE           | 2ND DEGREE | 4TH DEGREE |
| 1 DAY      | 0.1        | 0.3                  | 0.2        | 0.2        | 0.2        | 0.1        | 0.5                  | 0.3        | 0.2        | 0.2        | 0.2        | 0.2                  | 0.2        | 0.2        |
| 2 DAYS     | 0.2        | 0.4                  | 0.3        | 0.3        | 0.4        | 0.2        | 0.6                  | 0.5        | 0.4        | 0.4        | 0.4        | 0.4                  | 0.4        | 0.4        |
| 5 DAYS     | 0.4        | 0.7                  | 0.6        | 0.8        | 1.4        | 0.5        | 1.0                  | 0.9        | 0.9        | 1.0        | 1.0        | 0.9                  | 1.0        | 1.0        |
| 10 DAYS    | 1.1        | 1.2                  | 1.3        | 2.3        | 5.6        | 1.1        | 1.6                  | 1.7        | 2.4        | 1.1        | 1.6        | 1.7                  | 2.4        | 3.5        |
| 15 DAYS    | 2.2        | 1.7                  | 2.4        | 5.0        | 15.1       | 1.9        | 1.9                  | 2.7        | 5.1        | 1.9        | 1.9        | 2.7                  | 5.1        | 9.0        |
| 20 DAYS    | 3.4        | 2.1                  | 3.0        | 9.2        | 33.2       | 2.8        | 2.2                  | 3.8        | 9.1        | 2.8        | 2.2        | 3.8                  | 9.1        | 18.5       |
| 25 DAYS    | 4.9        | 2.5                  | 4.9        | 15.0       | 63.4       | 3.8        | 2.3                  | 5.0        | 13.5       | 3.8        | 2.3        | 5.0                  | 13.5       | 33.3       |
| 30 DAYS    | 5.2        | 2.3                  | 6.2        | 23.0       | 110.4      | 4.8        | 2.6                  | 6.2        | 20.0       | 4.8        | 2.6        | 6.2                  | 20.0       | 50.5       |
|            |            |                      |            |            |            |            |                      |            |            |            |            |                      |            |            |
| PREDICTION |            | CALIBRATION INTERVAL |            |            |            |            | CALIBRATION INTERVAL |            |            |            |            | CALIBRATION INTERVAL |            |            |
| LEAD TIME  | ARIMA      | 1ST DEGREE           | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA      | 1ST DEGREE           | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA      | 1ST DEGREE           | 2ND DEGREE | 4TH DEGREE |
| 1 DAY      | 0.1        | 0.7                  | 0.5        | 0.4        | 0.4        | 0.1        | 0.8                  | 0.9        | 0.6        | 0.4        | 0.2        | 0.9                  | 0.6        | 0.4        |
| 2 DAYS     | 0.2        | 0.7                  | 0.9        | 0.0        | 0.6        | 0.2        | 0.9                  | 1.1        | 0.8        | 0.0        | 0.0        | 0.8                  | 0.8        | 0.0        |
| 5 DAYS     | 0.5        | 0.9                  | 1.1        | 1.3        | 1.4        | 0.5        | 1.2                  | 1.5        | 1.4        | 1.2        | 1.5        | 1.5                  | 1.4        | 1.5        |
| 10 DAYS    | 1.1        | 1.3                  | 2.1        | 2.8        | 4.2        | 1.1        | 1.5                  | 2.3        | 2.4        | 1.1        | 1.5        | 2.3                  | 2.4        | 4.0        |
| 15 DAYS    | 1.9        | 1.7                  | 3.2        | 5.1        | 9.1        | 1.8        | 1.8                  | 3.0        | 3.8        | 1.8        | 1.8        | 3.0                  | 3.8        | 7.6        |
| 20 DAYS    | 2.2        | 2.0                  | 4.1        | 7.9        | 16.8       | 2.6        | 2.2                  | 3.6        | 5.5        | 2.6        | 2.2        | 3.6                  | 5.5        | 13.7       |
| 25 DAYS    | 3.0        | 2.4                  | 4.3        | 11.6       | 24.8       | 3.4        | 2.5                  | 4.1        | 7.6        | 3.4        | 2.5        | 4.1                  | 7.6        | 22.3       |
| 30 DAYS    | 3.2        | 3.0                  | 5.3        | 14.1       | 39.5       | 4.5        | 2.9                  | 4.8        | 10.2       | 4.5        | 2.9        | 4.8                  | 10.2       | 34.7       |

NOTE: THE RMS PREDICTION ERRORS ARE IN UNITS OF MICROSECONDS.

| PREDICTION | LEAD TIME | NUMBER OF SAMPLE INTERVALS |    |    |    |    |
|------------|-----------|----------------------------|----|----|----|----|
|            |           | 7                          | 14 | 21 | 28 | 42 |
| DAY        | 1         | 172                        | 84 | 56 | 40 | 28 |
|            | 2         | 172                        | 84 | 56 | 40 | 29 |
|            | 5         | 172                        | 84 | 56 | 40 | 29 |
|            | 10        | 172                        | 73 | 56 | 40 | 29 |
|            | 15        | 172                        | 79 | 55 | 33 | 23 |
|            | 20        | 171                        | 73 | 54 | 33 | 27 |
|            | 25        | 167                        | 77 | 54 | 37 | 25 |
|            | 30        | 167                        | 77 | 54 | 37 | 25 |

TABLE 9  
RMS PREDICTION ERRORS  
FOR  
HP RUBIDIUM FREQUENCY OSCILLATOR #229  
MODIFIED JULIAN DAY: 4-120 - 44350

| PREDICTION | LEAD TIME | CALIBRATION INTERVAL<br>7 DAYS  |            |            |            |            | CALIBRATION INTERVAL<br>14 DAYS |            |            |            |            |
|------------|-----------|---------------------------------|------------|------------|------------|------------|---------------------------------|------------|------------|------------|------------|
|            |           | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
|            | 1 DAY     | 0.1                             | 0.2        | 0.2        | 0.2        | 0.3        | 0.1                             | 0.3        | 0.2        | 0.2        | 0.2        |
|            | 2 DAYS    | 0.3                             | 0.3        | 0.4        | 0.5        | 1.1        | 0.2                             | 0.4        | 0.4        | 0.5        | 0.5        |
|            | 5 DAYS    | 0.7                             | 0.7        | 1.1        | 2.0        | 3.7        | 0.6                             | 0.7        | 0.8        | 1.5        | 2.0        |
|            | 10 DAYS   | 2.7                             | 1.2        | 3.1        | 12.0       | 73.9       | 1.4                             | 1.1        | 1.8        | 5.1        | 13.7       |
|            | 15 DAYS   | 5.3                             | 1.7        | 0.1        | 32.8       | 279.2      | 2.4                             | 1.8        | 3.2        | 12.0       | 43.3       |
|            | 20 DAYS   | 8.7                             | 2.5        | 10.1       | 69.3       | 751.7      | 3.7                             | 2.5        | 4.9        | 23.0       | 175.1      |
|            | 25 DAYS   | 13.1                            | 3.3        | 15.1       | 126.8      | 1603.7     | 5.5                             | 3.4        | 7.2        | 39.6       | 220.3      |
|            | 30 DAYS   | 13.5                            | 4.4        | 21.2       | 205.8      | 3247.1     | 7.5                             | 4.6        | 9.8        | 62.5       | 406.1      |
| PREDICTION | LEAD TIME | CALIBRATION INTERVAL<br>21 DAYS |            |            |            |            | CALIBRATION INTERVAL<br>28 DAYS |            |            |            |            |
|            |           | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
|            | 1 DAY     | 0.1                             | 0.4        | 0.4        | 0.3        | 0.3        | 0.1                             | 0.6        | 0.4        | 0.3        | 0.3        |
|            | 2 DAYS    | 0.3                             | 0.5        | 0.5        | 0.4        | 0.7        | 0.2                             | 0.7        | 0.5        | 0.5        | 0.5        |
|            | 5 DAYS    | 0.7                             | 0.8        | 0.9        | 1.2        | 2.9        | 0.6                             | 1.0        | 0.8        | 1.2        | 2.1        |
|            | 10 DAYS   | 1.5                             | 1.4        | 1.6        | 3.7        | 11.5       | 1.3                             | 1.7        | 1.5        | 3.2        | 7.4        |
|            | 15 DAYS   | 2.5                             | 2.1        | 2.5        | 8.1        | 31.1       | 2.0                             | 2.5        | 2.1        | 6.2        | 17.9       |
|            | 20 DAYS   | 3.9                             | 2.7        | 3.6        | 15.0       | 58.2       | 2.6                             | 3.5        | 2.9        | 10.4       | 36.4       |
|            | 25 DAYS   | 5.5                             | 3.9        | 4.9        | 24.9       | 130.7      | 3.6                             | 4.6        | 3.9        | 16.4       | 56.5       |
|            | 30 DAYS   | 7.2                             | 5.0        | 5.5        | 38.5       | 225.7      | 4.8                             | 5.8        | 4.9        | 24.1       | 110.8      |
| PREDICTION | LEAD TIME | CALIBRATION INTERVAL<br>42 DAYS |            |            |            |            | CALIBRATION INTERVAL<br>56 DAYS |            |            |            |            |
|            |           | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
|            | 1 DAY     | 0.1                             | 0.9        | 0.3        | 0.4        | 0.3        | 0.1                             | 1.6        | 0.4        | 0.4        | 0.5        |
|            | 2 DAYS    | 0.2                             | 1.1        | 0.4        | 0.6        | 0.4        | 0.2                             | 1.8        | 0.5        | 0.5        | 0.5        |
|            | 5 DAYS    | 0.4                             | 1.4        | 0.6        | 0.9        | 0.8        | 0.4                             | 2.4        | 0.7        | 0.8        | 1.4        |
|            | 10 DAYS   | 0.7                             | 2.3        | 0.9        | 1.2        | 2.0        | 0.7                             | 3.6        | 0.9        | 1.1        | 2.9        |
|            | 15 DAYS   | 1.1                             | 3.3        | 1.2        | 3.2        | 4.3        | 1.3                             | 4.8        | 1.0        | 1.8        | 5.3        |
|            | 20 DAYS   | 1.6                             | 4.4        | 1.6        | 4.8        | 8.2        | 1.7                             | 6.2        | 1.2        | 2.5        | 9.0        |
|            | 25 DAYS   | 2.3                             | 5.7        | 2.2        | 7.0        | 14.1       | 2.1                             | 7.7        | 1.5        | 3.4        | 14.3       |
|            | 30 DAYS   | 3.1                             | 7.2        | 2.6        | 10.0       | 22.7       | 2.7                             | 9.3        | 1.9        | 4.6        | 19.2       |

NOTE: THE RMS PREDICTION ERRORS ARE IN UNITS OF MICROSECONDS.

| PREDICTION | LEAD TIME | NUMBER OF SAMPLE INTERVALS |    |    |    |    |    |
|------------|-----------|----------------------------|----|----|----|----|----|
|            |           | 7                          | 14 | 21 | 28 | 42 | 56 |
| JAY        | 1         | 132                        | 64 | 44 | 32 | 20 | 15 |
|            | 2         | 132                        | 54 | 44 | 32 | 21 | 16 |
|            | 5         | 132                        | 54 | 44 | 32 | 20 | 15 |
|            | 10        | 132                        | 63 | 44 | 31 | 20 | 16 |
|            | 15        | 130                        | 61 | 43 | 31 | 20 | 16 |
|            | 20        | 129                        | 59 | 42 | 30 | 23 | 16 |
|            | 25        | 126                        | 55 | 41 | 29 | 23 | 15 |
|            | 30        | 122                        | 52 | 40 | 27 | 20 | 15 |

TABLE 10  
RMS PREDICTION ERRORS  
FOR  
HP CESIUM FREQUENCY OSCILLATOR #207  
MILLIFIED JULIAN DAY: 44120 - 44330

| PREDICTION | LEAD TIME | CALIBRATION INTERVAL<br>7 DAYS  |      |      |       |        | CALIBRATION INTERVAL<br>14 DAYS |        |        |        |        |
|------------|-----------|---------------------------------|------|------|-------|--------|---------------------------------|--------|--------|--------|--------|
|            |           | 1ST                             | 2ND  | 3RD  | 4TH   | ARIMA  | DEGREE                          | DEGREE | DEGREE | DEGREE | DEGREE |
|            | 1 DAY     | 0.02                            | 0.03 | 0.03 | 0.03  | 0.05   | 0.02                            | 0.04   | 0.03   | 0.03   | 0.04   |
|            | 2 DAYS    | 0.04                            | 0.04 | 0.05 | 0.03  | 0.17   | 0.03                            | 0.05   | 0.05   | 0.05   | 0.10   |
|            | 5 DAYS    | 0.15                            | 0.07 | 0.17 | 0.40  | 1.49   | 0.09                            | 0.07   | 0.10   | 0.18   | 0.55   |
|            | 10 DAYS   | 0.41                            | 0.14 | 0.45 | 1.78  | 11.55  | 0.23                            | 0.14   | 0.24   | 0.63   | 2.06   |
|            | 15 DAYS   | 0.79                            | 0.20 | 0.88 | 4.79  | 43.62  | 0.40                            | 0.20   | 0.44   | 1.49   | 8.53   |
|            | 20 DAYS   | 1.30                            | 0.27 | 1.44 | 10.04 | 118.03 | 0.52                            | 0.28   | 0.69   | 2.38   | 19.92  |
|            | 25 DAYS   | 1.95                            | 0.34 | 2.13 | 18.13 | 260.05 | 0.87                            | 0.36   | 0.94   | 4.70   | 33.86  |
|            | 30 DAYS   | 2.69                            | 0.40 | 2.87 | 28.22 | 483.22 | 1.19                            | 0.42   | 1.29   | 6.95   | 59.63  |
| PREDICTION | LEAD TIME | CALIBRATION INTERVAL<br>21 DAYS |      |      |       |        | CALIBRATION INTERVAL<br>28 DAYS |        |        |        |        |
|            |           | 1ST                             | 2ND  | 3RD  | 4TH   | ARIMA  | DEGREE                          | DEGREE | DEGREE | DEGREE | DEGREE |
|            | 1 DAY     | 0.02                            | 0.05 | 0.05 | 0.04  | 0.04   | 0.02                            | 0.06   | 0.04   | 0.04   | 0.05   |
|            | 2 DAYS    | 0.04                            | 0.07 | 0.07 | 0.06  | 0.08   | 0.03                            | 0.07   | 0.06   | 0.06   | 0.08   |
|            | 5 DAYS    | 0.08                            | 0.10 | 0.12 | 0.16  | 0.29   | 0.06                            | 0.08   | 0.10   | 0.14   | 0.23   |
|            | 10 DAYS   | 0.15                            | 0.16 | 0.24 | 0.42  | 1.19   | 0.12                            | 0.14   | 0.20   | 0.36   | 0.75   |
|            | 15 DAYS   | 0.23                            | 0.22 | 0.41 | 0.87  | 3.22   | 0.22                            | 0.19   | 0.33   | 0.71   | 1.85   |
|            | 20 DAYS   | 0.44                            | 0.28 | 0.62 | 1.59  | 6.64   | 0.36                            | 0.25   | 0.51   | 1.21   | 3.77   |
|            | 25 DAYS   | 0.66                            | 0.35 | 0.88 | 2.61  | 11.64  | 0.49                            | 0.34   | 0.69   | 1.39   | 6.44   |
|            | 30 DAYS   | 0.91                            | 0.43 | 1.10 | 3.97  | 17.31  | 0.67                            | 0.42   | 0.88   | 2.51   | 13.49  |
| PREDICTION | LEAD TIME | CALIBRATION INTERVAL<br>42 DAYS |      |      |       |        | CALIBRATION INTERVAL<br>56 DAYS |        |        |        |        |
|            |           | 1ST                             | 2ND  | 3RD  | 4TH   | ARIMA  | DEGREE                          | DEGREE | DEGREE | DEGREE | DEGREE |
|            | 1 DAY     | 0.01                            | 0.05 | 0.05 | 0.04  | 0.04   | 0.02                            | 0.14   | 0.08   | 0.07   | 0.03   |
|            | 2 DAYS    | 0.02                            | 0.07 | 0.06 | 0.05  | 0.05   | 0.02                            | 0.15   | 0.08   | 0.08   | 0.06   |
|            | 5 DAYS    | 0.07                            | 0.10 | 0.13 | 0.10  | 0.14   | 0.05                            | 0.19   | 0.12   | 0.15   | 0.12   |
|            | 10 DAYS   | 0.13                            | 0.10 | 0.13 | 0.24  | 0.42   | 0.12                            | 0.23   | 0.19   | 0.33   | 0.31   |
|            | 15 DAYS   | 0.25                            | 0.24 | 0.27 | 0.42  | 0.90   | 0.16                            | 0.32   | 0.27   | 0.53   | 0.62   |
|            | 20 DAYS   | 0.41                            | 0.31 | 0.39 | 0.68  | 1.59   | 0.24                            | 0.41   | 0.37   | 0.79   | 1.02   |
|            | 25 DAYS   | 0.57                            | 0.38 | 0.51 | 0.94  | 2.92   | 0.28                            | 0.48   | 0.38   | 0.79   | 1.73   |
|            | 30 DAYS   | 0.71                            | 0.47 | 0.62 | 1.30  | 4.57   | 0.31                            | 0.56   | 0.45   | 1.36   | 2.74   |

NOTE: THE RMS PREDICTION ERRORS ARE IN UNITS OF MICROSECONDS.

| PREDICTION | LEAD TIME | NUMBER OF SAMPLE INTERVALS |    |    |    |    |    |
|------------|-----------|----------------------------|----|----|----|----|----|
|            |           | 7                          | 14 | 21 | 28 | 42 | 56 |
|            | 1         | 120                        | 60 | 40 | 28 | 20 | 12 |
|            | 2         | 120                        | 60 | 40 | 28 | 20 | 12 |
|            | 5         | 120                        | 60 | 40 | 28 | 20 | 12 |
|            | 10        | 117                        | 53 | 40 | 28 | 20 | 12 |
|            | 15        | 117                        | 56 | 39 | 29 | 20 | 12 |
|            | 20        | 113                        | 53 | 37 | 27 | 20 | 11 |
|            | 25        | 113                        | 52 | 35 | 25 | 19 | 10 |
|            | 30        | 111                        | 51 | 33 | 24 | 19 | 10 |

TABLE II  
RMS PREDICTION ERRORS  
FJR  
HP CESIUM FREQUENCY OSCILLATOR #1114  
MODIFIED JULIAN DAY: 44236 - 44420

| PREDICTION<br>LEAD TIME | CALIBRATION INTERVAL<br>7 DAYS  |            |            |            |            | CALIBRATION INTERVAL<br>14 DAYS |            |            |            |            |
|-------------------------|---------------------------------|------------|------------|------------|------------|---------------------------------|------------|------------|------------|------------|
|                         | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
| 1 DAY                   | 0.01                            | 0.02       | 0.02       | 0.02       | 0.03       | 0.01                            | 0.02       | 0.02       | 0.02       | 0.02       |
| 2 DAYS                  | 0.03                            | 0.03       | 0.03       | 0.05       | 0.12       | 0.02                            | 0.03       | 0.03       | 0.03       | 0.04       |
| 5 DAYS                  | 0.09                            | 0.05       | 0.07       | 0.27       | 1.00       | 0.05                            | 0.04       | 0.05       | 0.11       | 0.17       |
| 10 DAYS                 | 0.26                            | 0.09       | 0.25       | 1.25       | 7.81       | 0.11                            | 0.06       | 0.12       | 0.41       | 0.87       |
| 15 DAYS                 | 0.53                            | 0.11       | 0.47       | 3.38       | 29.61      | 0.19                            | 0.08       | 0.20       | 0.94       | 2.76       |
| 20 DAYS                 | 0.84                            | 0.15       | 0.73       | 7.15       | 80.07      | 0.30                            | 0.10       | 0.31       | 1.79       | 6.42       |
| 25 DAYS                 | 1.27                            | 0.18       | 1.18       | 13.03      | 177.59     | 0.45                            | 0.12       | 0.46       | 3.12       | 12.86      |
| 30 DAYS                 | 1.73                            | 0.22       | 1.65       | 21.52      | 342.54     | 0.61                            | 0.14       | 0.64       | 4.84       | 23.70      |
| <br>                    |                                 |            |            |            |            |                                 |            |            |            |            |
| PREDICTION<br>LEAD TIME | CALIBRATION INTERVAL<br>21 DAYS |            |            |            |            | CALIBRATION INTERVAL<br>28 DAYS |            |            |            |            |
|                         | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
| 1 DAY                   | 0.01                            | 0.02       | 0.03       | 0.03       | 0.02       | 0.01                            | 0.03       | 0.02       | 0.03       | 0.03       |
| 2 DAYS                  | 0.02                            | 0.03       | 0.04       | 0.05       | 0.05       | 0.01                            | 0.03       | 0.02       | 0.04       | 0.05       |
| 5 DAYS                  | 0.04                            | 0.04       | 0.07       | 0.12       | 0.18       | 0.04                            | 0.04       | 0.04       | 0.10       | 0.18       |
| 10 DAYS                 | 0.09                            | 0.05       | 0.13       | 0.31       | 0.78       | 0.10                            | 0.05       | 0.08       | 0.22       | 0.63       |
| 15 DAYS                 | 0.15                            | 0.03       | 0.21       | 0.65       | 2.19       | 0.16                            | 0.07       | 0.11       | 0.42       | 1.47       |
| 20 DAYS                 | 0.22                            | 0.10       | 0.30       | 1.17       | 4.92       | 0.22                            | 0.10       | 0.15       | 0.70       | 2.98       |
| 25 DAYS                 | 0.31                            | 0.12       | 0.42       | 1.97       | 10.07      | 0.31                            | 0.14       | 0.21       | 1.08       | 5.40       |
| 30 DAYS                 | 0.42                            | 0.13       | 0.55       | 3.01       | 17.73      | 0.39                            | 0.16       | 0.27       | 1.57       | 9.00       |
| <br>                    |                                 |            |            |            |            |                                 |            |            |            |            |
| PREDICTION<br>LEAD TIME | CALIBRATION INTERVAL<br>42 DAYS |            |            |            |            | CALIBRATION INTERVAL<br>56 DAYS |            |            |            |            |
|                         | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
| 1 DAY                   | 0.01                            | 0.03       | 0.01       | 0.03       | 0.03       | 0.01                            | 0.05       | 0.03       | 0.02       | 0.03       |
| 2 DAYS                  | 0.02                            | 0.03       | 0.02       | 0.04       | 0.04       | 0.01                            | 0.06       | 0.03       | 0.03       | 0.04       |
| 5 DAYS                  | 0.06                            | 0.04       | 0.04       | 0.09       | 0.10       | 0.03                            | 0.07       | 0.04       | 0.04       | 0.06       |
| 10 DAYS                 | 0.13                            | 0.07       | 0.06       | 0.16       | 0.21       | 0.07                            | 0.09       | 0.06       | 0.08       | 0.13       |
| 15 DAYS                 | 0.16                            | 0.06       | 0.11       | 0.26       | 0.34       | 0.10                            | 0.11       | 0.08       | 0.13       | 0.24       |
| 20 DAYS                 | 0.22                            | 0.09       | 0.14       | 0.38       | 0.59       | 0.14                            | 0.13       | 0.12       | 0.19       | 0.41       |
| 25 DAYS                 | 0.29                            | 0.11       | 0.17       | 0.54       | 0.95       | 0.18                            | 0.17       | 0.17       | 0.26       | 0.63       |
| 30 DAYS                 | 0.43                            | 0.14       | 0.23       | 0.70       | 1.51       | 0.25                            | 0.21       | 0.23       | 0.34       | 0.83       |

NOTE: THE RMS PREDICTION ERRORS ARE IN UNITS OF MICROSECONDS.

| PREDICTION<br>LEAD TIME | NUMBER OF SAMPLE INTERVALS |    |    |    |    |    |
|-------------------------|----------------------------|----|----|----|----|----|
|                         | 7                          | 14 | 21 | 28 | 42 |    |
| DAY 1                   | 104                        | 52 | 32 | 24 | 16 | 12 |
| 2                       | 104                        | 52 | 32 | 24 | 16 | 12 |
| 5                       | 104                        | 52 | 32 | 24 | 16 | 12 |
| 10                      | 102                        | 52 | 31 | 24 | 15 | 12 |
| 15                      | 102                        | 51 | 30 | 23 | 14 | 12 |
| 20                      | 97                         | 49 | 29 | 23 | 14 | 11 |
| 25                      | 95                         | 45 | 25 | 23 | 14 | 11 |
| 30                      | 93                         | 43 | 23 | 23 | 13 | 10 |

TABLE 12  
RMS PREDICTION ERRORS  
FOR  
HP CESIUM FREQUENCY OSCILLATOR #875  
MODIFIED JULIAN DAY: 44236 - 44391

| PREDICTION | LEAD TIME | CALIBRATION INTERVAL<br>7 DAYS  |            |            |            |            | CALIBRATION INTERVAL<br>14 DAYS |            |            |            |            |
|------------|-----------|---------------------------------|------------|------------|------------|------------|---------------------------------|------------|------------|------------|------------|
|            |           | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
|            | 1 DAY     | 0.02                            | 0.02       | 0.02       | 0.02       | 0.04       | 0.02                            | 0.02       | 0.02       | 0.02       | 0.03       |
|            | 2 DAYS    | 0.03                            | 0.03       | 0.03       | 0.03       | 0.15       | 0.03                            | 0.03       | 0.03       | 0.04       | 0.03       |
|            | 5 DAYS    | 0.09                            | 0.04       | 0.08       | 0.32       | 1.26       | 0.08                            | 0.04       | 0.06       | 0.12       | 0.30       |
|            | 10 DAYS   | 0.27                            | 0.03       | 0.22       | 1.47       | 7.30       | 0.19                            | 0.08       | 0.13       | 0.41       | 1.43       |
|            | 15 DAYS   | 0.55                            | 0.12       | 0.44       | 4.06       | 34.14      | 0.28                            | 0.12       | 0.23       | 0.92       | 4.20       |
|            | 20 DAYS   | 0.85                            | 0.15       | 0.71       | 8.53       | 83.67      | 0.45                            | 0.15       | 0.35       | 1.77       | 9.94       |
|            | 25 DAYS   | 1.30                            | 0.21       | 1.07       | 15.59      | 195.10     | 0.58                            | 0.21       | 0.51       | 3.07       | 20.51      |
|            | 30 DAYS   | 1.82                            | 0.25       | 1.52       | 25.84      | 379.09     | 0.93                            | 0.25       | 0.69       | 4.57       | 37.95      |
| PREDICTION | LEAD TIME | CALIBRATION INTERVAL<br>21 DAYS |            |            |            |            | CALIBRATION INTERVAL<br>28 DAYS |            |            |            |            |
|            |           | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
|            | 1 DAY     | 0.01                            | 0.04       | 0.03       | 0.02       | 0.02       | 0.01                            | 0.04       | 0.03       | 0.02       | 0.03       |
|            | 2 DAYS    | 0.03                            | 0.04       | 0.03       | 0.04       | 0.06       | 0.02                            | 0.05       | 0.04       | 0.04       | 0.05       |
|            | 5 DAYS    | 0.07                            | 0.05       | 0.06       | 0.11       | 0.22       | 0.05                            | 0.07       | 0.06       | 0.09       | 0.13       |
|            | 10 DAYS   | 0.17                            | 0.08       | 0.13       | 0.30       | 0.87       | 0.08                            | 0.11       | 0.11       | 0.20       | 0.45       |
|            | 15 DAYS   | 0.29                            | 0.11       | 0.20       | 0.60       | 2.31       | 0.14                            | 0.14       | 0.16       | 0.40       | 1.11       |
|            | 20 DAYS   | 0.43                            | 0.14       | 0.32       | 1.10       | 5.16       | 0.21                            | 0.18       | 0.22       | 0.59       | 2.24       |
|            | 25 DAYS   | 0.65                            | 0.19       | 0.45       | 1.83       | 19.18      | 0.30                            | 0.22       | 0.30       | 1.08       | 4.03       |
|            | 30 DAYS   | 0.92                            | 0.22       | 0.61       | 2.75       | 18.01      | 0.37                            | 0.27       | 0.38       | 1.54       | 6.84       |
| PREDICTION | LEAD TIME | CALIBRATION INTERVAL<br>42 DAYS |            |            |            |            | CALIBRATION INTERVAL<br>56 DAYS |            |            |            |            |
|            |           | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
|            | 1 DAY     | 0.01                            | 0.05       | 0.03       | 0.02       | 0.03       | 0.01                            | 0.06       | 0.04       | 0.02       | 0.03       |
|            | 2 DAYS    | 0.02                            | 0.07       | 0.04       | 0.04       | 0.05       | 0.01                            | 0.06       | 0.05       | 0.03       | 0.04       |
|            | 5 DAYS    | 0.04                            | 0.03       | 0.05       | 0.07       | 0.12       | 0.03                            | 0.09       | 0.06       | 0.07       | 0.08       |
|            | 10 DAYS   | 0.09                            | 0.11       | 0.10       | 0.15       | 0.33       | 0.06                            | 0.11       | 0.11       | 0.13       | 0.23       |
|            | 15 DAYS   | 0.16                            | 0.14       | 0.15       | 0.26       | 0.70       | 0.10                            | 0.14       | 0.17       | 0.20       | 0.40       |
|            | 20 DAYS   | 0.23                            | 0.13       | 0.21       | 0.41       | 1.27       | 0.16                            | 0.17       | 0.24       | 0.34       | 0.67       |
|            | 25 DAYS   | 0.34                            | 0.21       | 0.30       | 0.59       | 2.09       | 0.19                            | 0.20       | 0.31       | 0.53       | 1.04       |
|            | 30 DAYS   | 0.50                            | 0.22       | 0.40       | 0.86       | 3.28       | 0.28                            | 0.20       | 0.37       | 0.72       | 1.71       |

NOTE: THE RMS PREDICTION ERRORS ARE IN UNITS OF MICROSECONDS.

| PREDICTION | LEAD TIME | NUMBER OF SAMPLE INTERVALS |    |    |    |    |    |
|------------|-----------|----------------------------|----|----|----|----|----|
|            |           | 7                          | 14 | 21 | 28 | 42 | 56 |
|            | 1         | 83                         | 44 | 28 | 20 | 12 | 8  |
|            | 2         | 83                         | 44 | 28 | 20 | 12 | 8  |
|            | 5         | 33                         | 44 | 28 | 20 | 12 | 8  |
|            | 10        | 37                         | 44 | 28 | 19 | 12 | 8  |
|            | 15        | 31                         | 42 | 28 | 19 | 12 | 8  |
|            | 20        | 77                         | 42 | 26 | 19 | 12 | 7  |
|            | 25        | 77                         | 40 | 24 | 17 | 12 | 6  |
|            | 30        | 74                         | 39 | 23 | 13 | 12 | 5  |

TABLE 13  
RMS PREDICTION ERRORS  
FOR  
HP CESIUM FREQUENCY OSCILLATOR #549  
MODIFIED JULIAN DAY: 44120 - 44330

| PREDICTION | LEAD TIME | CALIBRATION INTERVAL<br>7 DAYS  |      |      |       |        | CALIBRATION INTERVAL<br>14 DAYS |      |      |      |       |
|------------|-----------|---------------------------------|------|------|-------|--------|---------------------------------|------|------|------|-------|
|            |           | 1ST                             | 2ND  | 3RD  | 4TH   | ARIMA  | DEGREE                          | 1ST  | 2ND  | 3RD  | 4TH   |
|            | 1 DAY     | 0.02                            | 0.02 | 0.02 | 0.02  | 0.02   | 0.02                            | 0.03 | 0.02 | 0.02 | 0.03  |
|            | 2 DAYS    | 0.04                            | 0.03 | 0.05 | 0.06  | 0.03   | 0.03                            | 0.03 | 0.04 | 0.04 | 0.05  |
|            | 5 DAYS    | 0.12                            | 0.09 | 0.13 | 0.32  | 0.36   | 0.07                            | 0.05 | 0.09 | 0.14 | 0.23  |
|            | 10 DAYS   | 0.37                            | 0.10 | 0.40 | 1.49  | 1.46   | 0.16                            | 0.08 | 0.20 | 0.40 | 1.49  |
|            | 15 DAYS   | 0.71                            | 0.15 | 0.77 | 4.06  | 3.73   | 0.30                            | 0.12 | 0.35 | 1.05 | 4.63  |
|            | 20 DAYS   | 1.19                            | 0.21 | 1.27 | 8.57  | 107.87 | 0.48                            | 0.16 | 0.55 | 1.79 | 11.07 |
|            | 25 DAYS   | 1.73                            | 0.26 | 1.89 | 15.61 | 233.95 | 0.71                            | 0.19 | 0.72 | 3.34 | 21.21 |
|            | 30 DAYS   | 2.43                            | 0.29 | 2.59 | 24.75 | 451.87 | 0.96                            | 0.21 | 0.89 | 4.95 | 35.25 |
| PREDICTION | LEAD TIME | CALIBRATION INTERVAL<br>21 DAYS |      |      |       |        | CALIBRATION INTERVAL<br>28 DAYS |      |      |      |       |
|            |           | 1ST                             | 2ND  | 3RD  | 4TH   | ARIMA  | DEGREE                          | 1ST  | 2ND  | 3RD  | 4TH   |
|            | 1 DAY     | 0.02                            | 0.03 | 0.03 | 0.04  | 0.03   | 0.02                            | 0.04 | 0.03 | 0.03 | 0.04  |
|            | 2 DAYS    | 0.03                            | 0.04 | 0.04 | 0.07  | 0.07   | 0.03                            | 0.05 | 0.04 | 0.04 | 0.05  |
|            | 5 DAYS    | 0.09                            | 0.05 | 0.07 | 0.18  | 0.23   | 0.06                            | 0.07 | 0.06 | 0.09 | 0.13  |
|            | 10 DAYS   | 0.19                            | 0.10 | 0.12 | 0.47  | 0.96   | 0.12                            | 0.11 | 0.09 | 0.19 | 0.57  |
|            | 15 DAYS   | 0.23                            | 0.14 | 0.19 | 0.98  | 2.03   | 0.20                            | 0.13 | 0.17 | 0.33 | 1.35  |
|            | 20 DAYS   | 0.34                            | 0.13 | 0.23 | 1.67  | 4.04   | 0.29                            | 0.17 | 0.25 | 0.62 | 2.80  |
|            | 25 DAYS   | 0.43                            | 0.22 | 0.39 | 2.32  | 9.06   | 0.42                            | 0.20 | 0.34 | 0.98 | 4.84  |
|            | 30 DAYS   | 0.63                            | 0.25 | 0.49 | 3.10  | 15.07  | 0.52                            | 0.21 | 0.47 | 1.36 | 6.49  |
| PREDICTION | LEAD TIME | CALIBRATION INTERVAL<br>42 DAYS |      |      |       |        | CALIBRATION INTERVAL<br>56 DAYS |      |      |      |       |
|            |           | 1ST                             | 2ND  | 3RD  | 4TH   | ARIMA  | DEGREE                          | 1ST  | 2ND  | 3RD  | 4TH   |
|            | 1 DAY     | 0.02                            | 0.05 | 0.04 | 0.03  | 0.03   | 0.02                            | 0.08 | 0.06 | 0.04 | 0.03  |
|            | 2 DAYS    | 0.03                            | 0.04 | 0.05 | 0.05  | 0.04   | 0.03                            | 0.08 | 0.07 | 0.05 | 0.05  |
|            | 5 DAYS    | 0.09                            | 0.05 | 0.03 | 0.09  | 0.10   | 0.06                            | 0.08 | 0.10 | 0.12 | 0.11  |
|            | 10 DAYS   | 0.19                            | 0.09 | 0.14 | 0.20  | 0.25   | 0.10                            | 0.13 | 0.15 | 0.22 | 0.27  |
|            | 15 DAYS   | 0.23                            | 0.12 | 0.22 | 0.36  | 0.51   | 0.10                            | 0.16 | 0.21 | 0.38 | 0.51  |
|            | 20 DAYS   | 0.34                            | 0.15 | 0.30 | 0.55  | 0.96   | 0.25                            | 0.10 | 0.27 | 0.51 | 0.93  |
|            | 25 DAYS   | 0.43                            | 0.19 | 0.28 | 0.84  | 1.51   | 0.35                            | 0.20 | 0.32 | 0.90 | 1.54  |
|            | 30 DAYS   | 0.63                            | 0.20 | 0.48 | 1.15  | 2.42   | 0.43                            | 0.22 | 0.38 | 1.24 | 2.29  |

NOTE: THE RMS PREDICTION ERRORS ARE IN UNITS OF MICROSECONDS.

NUMBER OF SAMPLE INTERVALS

| PREDICTION | LEAD TIME | 7   | 14 | CALIBRATION INTERVAL |    | 56 |
|------------|-----------|-----|----|----------------------|----|----|
|            |           |     |    | 21                   | 28 |    |
| DAY        | 1         | 120 | 60 | 40                   | 23 | 20 |
|            | 2         | 120 | 60 | 40                   | 23 | 12 |
|            | 5         | 120 | 50 | 40                   | 23 | 12 |
|            | 10        | 119 | 53 | 40                   | 23 | 12 |
|            | 15        | 117 | 55 | 37                   | 23 | 12 |
|            | 20        | 115 | 55 | 37                   | 27 | 11 |
|            | 25        | 113 | 52 | 35                   | 25 | 10 |
|            | 30        | 111 | 51 | 33                   | 24 | 10 |

TABLE 14  
RMS PREDICTION ERRORS  
FOR  
HP CESIUM FREQUENCY OSCILLATOR #1254  
MODIFIED JULIAN DAY: 44120 - 44350

| PREDICTION<br>LEAD TIME | ARIMA | CALIBRATION INTERVAL<br>7 DAYS  |               |               |               | CALIBRATION INTERVAL<br>14 DAYS |               |               |               |
|-------------------------|-------|---------------------------------|---------------|---------------|---------------|---------------------------------|---------------|---------------|---------------|
|                         |       | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE |
| 1 DAY                   | 0.02  | 0.02                            | 0.02          | 0.03          | 0.05          | 0.02                            | 0.02          | 0.02          | 0.03          |
| 2 DAYS                  | 0.04  | 0.02                            | 0.04          | 0.07          | 0.16          | 0.04                            | 0.03          | 0.03          | 0.07          |
| 5 DAYS                  | 0.11  | 0.05                            | 0.11          | 0.35          | 1.37          | 0.09                            | 0.05          | 0.06          | 0.12          |
| 10 DAYS                 | 0.31  | 0.09                            | 0.27          | 1.63          | 10.68         | 0.21                            | 0.07          | 0.13          | 0.42          |
| 15 DAYS                 | 0.60  | 0.13                            | 0.56          | 4.44          | 39.23         | 0.40                            | 0.09          | 0.23          | 0.99          |
| 20 DAYS                 | 0.95  | 0.17                            | 0.93          | 9.38          | 105.59        | 0.65                            | 0.12          | 0.36          | 1.74          |
| 25 DAYS                 | 1.42  | 0.21                            | 1.31          | 16.72         | 224.65        | 0.92                            | 0.15          | 0.52          | 3.25          |
| 30 DAYS                 | 2.00  | 0.25                            | 1.85          | 27.78         | 431.36        | 1.29                            | 0.18          | 0.73          | 4.25          |
| PREDICTION<br>LEAD TIME | ARIMA | CALIBRATION INTERVAL<br>21 DAYS |               |               |               | CALIBRATION INTERVAL<br>28 DAYS |               |               |               |
|                         |       | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE |
| 1 DAY                   | 0.01  | 0.03                            | 0.03          | 0.02          | 0.02          | 0.02                            | 0.03          | 0.03          | 0.03          |
| 2 DAYS                  | 0.02  | 0.04                            | 0.04          | 0.04          | 0.04          | 0.03                            | 0.04          | 0.04          | 0.05          |
| 5 DAYS                  | 0.05  | 0.05                            | 0.07          | 0.10          | 0.15          | 0.05                            | 0.05          | 0.06          | 0.09          |
| 10 DAYS                 | 0.13  | 0.09                            | 0.13          | 0.30          | 0.30          | 0.10                            | 0.08          | 0.11          | 0.21          |
| 15 DAYS                 | 0.29  | 0.12                            | 0.21          | 0.55          | 1.51          | 0.17                            | 0.11          | 0.17          | 0.39          |
| 20 DAYS                 | 0.33  | 0.14                            | 0.32          | 1.21          | 3.51          | 0.23                            | 0.13          | 0.23          | 0.69          |
| 25 DAYS                 | 0.51  | 0.17                            | 0.44          | 2.02          | 5.69          | 0.34                            | 0.16          | 0.31          | 1.07          |
| 30 DAYS                 | 0.69  | 0.21                            | 0.58          | 3.11          | 11.69         | 0.45                            | 0.20          | 0.39          | 1.56          |
| PREDICTION<br>LEAD TIME | ARIMA | CALIBRATION INTERVAL<br>42 DAYS |               |               |               | CALIBRATION INTERVAL<br>56 DAYS |               |               |               |
|                         |       | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE |
| 1 DAY                   | 0.02  | 0.03                            | 0.03          | 0.03          | 0.03          | 0.02                            | 0.03          | 0.04          | 0.03          |
| 2 DAYS                  | 0.03  | 0.03                            | 0.04          | 0.04          | 0.04          | 0.02                            | 0.06          | 0.04          | 0.05          |
| 5 DAYS                  | 0.05  | 0.05                            | 0.05          | 0.07          | 0.08          | 0.05                            | 0.08          | 0.05          | 0.11          |
| 10 DAYS                 | 0.09  | 0.08                            | 0.09          | 0.13          | 0.19          | 0.08                            | 0.11          | 0.09          | 0.16          |
| 15 DAYS                 | 0.14  | 0.10                            | 0.14          | 0.22          | 0.39          | 0.12                            | 0.14          | 0.11          | 0.26          |
| 20 DAYS                 | 0.20  | 0.13                            | 0.13          | 0.35          | 0.75          | 0.17                            | 0.16          | 0.14          | 0.39          |
| 25 DAYS                 | 0.28  | 0.15                            | 0.22          | 0.54          | 1.29          | 0.22                            | 0.19          | 0.19          | 0.54          |
| 30 DAYS                 | 0.35  | 0.18                            | 0.23          | 0.76          | 2.04          | 0.26                            | 0.23          | 0.25          | 0.69          |

NOTE: THE RMS PREDICTION ERRORS ARE IN UNITS OF MICROSECONDS.

NUMBER OF SAMPLE INTERVALS

| PREDICTION<br>LEAD TIME | 7   | 14  | CALIBRATION INTERVAL |    |    | 56 |    |
|-------------------------|-----|-----|----------------------|----|----|----|----|
|                         |     |     | 21                   | 28 | 42 |    |    |
| DAY                     | 1   | 132 | 54                   | 44 | 32 | 20 | 16 |
| 2                       | 132 | 54  | 44                   | 32 | 20 | 16 | 16 |
| 5                       | 132 | 54  | 44                   | 32 | 20 | 16 | 16 |
| 10                      | 132 | 53  | 44                   | 31 | 20 | 16 | 16 |
| 15                      | 130 | 51  | 43                   | 31 | 20 | 16 | 16 |
| 20                      | 129 | 50  | 42                   | 30 | 20 | 16 | 16 |
| 25                      | 126 | 55  | 41                   | 29 | 20 | 15 | 15 |
| 30                      | 122 | 52  | 40                   | 29 | 20 | 15 | 15 |

TABLE 15

RMS PREDICTION ERRORS  
 FOR  
 FTS CESIUM FREQUENCY OSCILLATOR MODEL 4350 #107  
 MODIFIED JULIAN DAY: 44297 - 44429

| PREDICTION<br>LEAD TIME | CALIBRATION INTERVAL<br>7 DAYS  |            |            |            |            | CALIBRATION INTERVAL<br>14 DAYS |            |            |            |            |
|-------------------------|---------------------------------|------------|------------|------------|------------|---------------------------------|------------|------------|------------|------------|
|                         | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
| 1 DAY                   | 0.01                            | 0.01       | 0.01       | 0.01       | 0.03       | 0.01                            | 0.01       | 0.01       | 0.01       | 0.01       |
| 2 DAYS                  | 0.02                            | 0.01       | 0.02       | 0.03       | 0.08       | 0.01                            | 0.02       | 0.02       | 0.02       | 0.03       |
| 5 DAYS                  | 0.05                            | 0.02       | 0.05       | 0.17       | 0.59       | 0.03                            | 0.03       | 0.04       | 0.07       | 0.14       |
| 10 DAYS                 | 0.17                            | 0.05       | 0.15       | 0.75       | 5.19       | 0.08                            | 0.04       | 0.07       | 0.25       | 0.77       |
| 15 DAYS                 | 0.32                            | 0.07       | 0.23       | 2.10       | 19.10      | 0.15                            | 0.07       | 0.14       | 0.57       | 2.42       |
| 20 DAYS                 | 0.50                            | 0.10       | 0.44       | 4.47       | 50.91      | 0.24                            | 0.10       | 0.23       | 1.08       | 5.60       |
| 25 DAYS                 | 0.75                            | 0.13       | 0.65       | 8.18       | 112.59     | 0.36                            | 0.13       | 0.33       | 1.77       | 11.49      |
| 30 DAYS                 | 1.04                            | 0.17       | 0.91       | 13.45      | 219.39     | 0.50                            | 0.17       | 0.46       | 2.79       | 20.57      |
| PREDICTION<br>LEAD TIME | CALIBRATION INTERVAL<br>21 DAYS |            |            |            |            | CALIBRATION INTERVAL<br>28 DAYS |            |            |            |            |
|                         | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
| 1 DAY                   | 0.01                            | 0.01       | 0.01       | 0.01       | 0.01       | 0.01                            | 0.02       | 0.02       | 0.01       | 0.01       |
| 2 DAYS                  | 0.01                            | 0.02       | 0.02       | 0.02       | 0.03       | 0.01                            | 0.03       | 0.02       | 0.01       | 0.02       |
| 5 DAYS                  | 0.03                            | 0.02       | 0.03       | 0.05       | 0.10       | 0.02                            | 0.04       | 0.04       | 0.04       | 0.06       |
| 10 DAYS                 | 0.05                            | 0.04       | 0.05       | 0.15       | 0.43       | 0.06                            | 0.06       | 0.07       | 0.11       | 0.18       |
| 15 DAYS                 | 0.11                            | 0.05       | 0.09       | 0.32       | 1.17       | 0.12                            | 0.09       | 0.12       | 0.22       | 0.45       |
| 20 DAYS                 | 0.18                            | 0.07       | 0.14       | 0.60       | 2.60       | 0.20                            | 0.13       | 0.17       | 0.39       | 0.91       |
| 25 DAYS                 | 0.25                            | 0.10       | 0.20       | 0.96       | 4.96       | 0.29                            | 0.16       | 0.23       | 0.63       | 1.64       |
| 30 DAYS                 | 0.33                            | 0.13       | 0.29       | 1.51       | 9.06       | 0.40                            | 0.20       | 0.29       | 0.96       | 2.76       |
| PREDICTION<br>LEAD TIME | CALIBRATION INTERVAL<br>42 DAYS |            |            |            |            | CALIBRATION INTERVAL<br>56 DAYS |            |            |            |            |
|                         | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
| 1 DAY                   | 0.01                            | 0.04       | 0.01       | 0.01       | 0.02       | 0.01                            | 0.06       | 0.03       | 0.02       | 0.02       |
| 2 DAYS                  | 0.01                            | 0.04       | 0.02       | 0.02       | 0.03       | 0.01                            | 0.16       | 0.04       | 0.02       | 0.02       |
| 5 DAYS                  | 0.02                            | 0.06       | 0.03       | 0.04       | 0.06       | 0.02                            | 0.08       | 0.05       | 0.04       | 0.04       |
| 10 DAYS                 | 0.05                            | 0.08       | 0.05       | 0.08       | 0.15       | 0.04                            | 0.10       | 0.08       | 0.09       | 0.11       |
| 15 DAYS                 | 0.09                            | 0.12       | 0.08       | 0.14       | 0.33       | 0.07                            | 0.12       | 0.12       | 0.14       | 0.22       |
| 20 DAYS                 | 0.13                            | 0.14       | 0.12       | 0.24       | 0.62       | 0.11                            | 0.14       | 0.16       | 0.23       | 0.34       |
| 25 DAYS                 | 0.20                            | 0.17       | 0.15       | 0.37       | 1.07       | 0.17                            | 0.15       | 0.21       | 0.33       | 0.46       |
| 30 DAYS                 | 0.28                            | 0.20       | 0.19       | 0.54       | 1.69       | 0.23                            | 0.17       | 0.26       | 0.46       | 0.67       |

NOTE: THE RMS PREDICTION ERRORS ARE IN UNITS OF MICROSECONDS.

## NUMBER OF SAMPLE INTERVALS

| PREDICTION<br>LEAD TIME | 7  | 14 | CALIBRATION INTERVAL |    |    |    |   |
|-------------------------|----|----|----------------------|----|----|----|---|
|                         |    |    | 21                   | 23 | 42 |    |   |
| DAY                     | 1  | 75 | 35                   | 24 | 15 | 12 | 3 |
|                         | 2  | 75 | 36                   | 24 | 15 | 12 | 3 |
|                         | 5  | 75 | 36                   | 24 | 16 | 12 | 3 |
|                         | 10 | 74 | 35                   | 24 | 15 | 12 | 3 |
|                         | 15 | 70 | 34                   | 22 | 15 | 10 | 8 |
|                         | 20 | 69 | 33                   | 21 | 15 | 10 | 7 |
|                         | 25 | 62 | 23                   | 21 | 15 | 9  | 5 |
|                         | 30 | 51 | 27                   | 19 | 14 | 3  | 5 |

TABLE 16  
RMS PREDICTION ERRORS  
FOR  
FTS CESIUM FREQUENCY OSCILLATOR MODEL 4050 #108  
MODIFIED JULIAN DAY: 44305 - 44429

| PREDICTION | LEAD TIME | CALIBRATION INTERVAL<br>7 DAYS  |            |            |            |            | CALIBRATION INTERVAL<br>14 DAYS |            |            |            |            |
|------------|-----------|---------------------------------|------------|------------|------------|------------|---------------------------------|------------|------------|------------|------------|
|            |           | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
|            | 1 DAY     | 0.02                            | 0.03       | 0.02       | 0.03       | 0.06       | 0.01                            | 0.04       | 0.04       | 0.03       | 0.03       |
|            | 2 DAYS    | 0.04                            | 0.04       | 0.04       | 0.08       | 0.20       | 0.03                            | 0.06       | 0.05       | 0.05       | 0.07       |
|            | 5 DAYS    | 0.14                            | 0.08       | 0.14       | 0.37       | 1.72       | 0.08                            | 0.10       | 0.11       | 0.21       | 0.32       |
|            | 10 DAYS   | 0.42                            | 0.17       | 0.42       | 1.75       | 13.16      | 0.21                            | 0.19       | 0.28       | 0.71       | 1.87       |
|            | 15 DAYS   | 0.83                            | 0.28       | 0.60       | 4.86       | 50.59      | 0.40                            | 0.25       | 0.56       | 1.08       | 5.67       |
|            | 20 DAYS   | 1.41                            | 0.35       | 1.33       | 10.06      | 136.84     | 0.59                            | 0.23       | 0.39       | 3.44       | 13.84      |
|            | 25 DAYS   | 2.14                            | 0.35       | 1.90       | 18.23      | 300.40     | 0.92                            | 0.23       | 1.24       | 5.78       | 28.34      |
|            | 30 DAYS   | 2.95                            | 0.38       | 2.09       | 30.16      | 584.95     | 0.95                            | 0.23       | 1.12       | 8.45       | 52.81      |
| PREDICTION | LEAD TIME | CALIBRATION INTERVAL<br>21 DAYS |            |            |            |            | CALIBRATION INTERVAL<br>28 DAYS |            |            |            |            |
|            |           | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
|            | 1 DAY     | 0.02                            | 0.05       | 0.05       | 0.03       | 0.04       | 0.02                            | 0.08       | 0.09       | 0.04       | 0.04       |
|            | 2 DAYS    | 0.03                            | 0.07       | 0.07       | 0.04       | 0.08       | 0.03                            | 0.10       | 0.12       | 0.07       | 0.08       |
|            | 5 DAYS    | 0.09                            | 0.12       | 0.13       | 0.14       | 0.32       | 0.08                            | 0.15       | 0.21       | 0.19       | 0.25       |
|            | 10 DAYS   | 0.21                            | 0.22       | 0.25       | 0.42       | 1.23       | 0.23                            | 0.28       | 0.43       | 0.55       | 0.80       |
|            | 15 DAYS   | 0.38                            | 0.13       | 0.32       | 1.00       | 3.33       | 0.37                            | 0.21       | 0.41       | 1.09       | 1.74       |
|            | 20 DAYS   | 0.60                            | 0.20       | 0.46       | 1.91       | 7.14       | 0.54                            | 0.20       | 0.56       | 1.35       | 3.33       |
|            | 25 DAYS   | 0.87                            | 0.19       | 0.59       | 3.13       | 13.44      | 0.47                            | 0.22       | 0.61       | 1.75       | 5.64       |
|            | 30 DAYS   | 1.05                            | 0.24       | 0.74       | 2.94       | 18.57      | 0.53                            | 0.21       | 0.65       | 2.54       | 7.35       |
| PREDICTION | LEAD TIME | CALIBRATION INTERVAL<br>42 DAYS |            |            |            |            | CALIBRATION INTERVAL<br>56 DAYS |            |            |            |            |
|            |           | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA                           | 1ST DEGREE | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |
|            | 1 DAY     | 0.01                            | 0.07       | 0.07       | 0.06       | 0.03       | 0.03                            | 0.09       | 0.08       | 0.09       | 0.06       |
|            | 2 DAYS    | 0.03                            | 0.07       | 0.08       | 0.08       | 0.06       | 0.03                            | 0.10       | 0.09       | 0.10       | 0.07       |
|            | 5 DAYS    | 0.07                            | 0.08       | 0.14       | 0.16       | 0.18       | 0.07                            | 0.15       | 0.12       | 0.17       | 0.16       |
|            | 10 DAYS   | 0.13                            | 0.15       | 0.29       | 0.38       | 0.54       | 0.16                            | 0.21       | 0.15       | 0.32       | 0.46       |
|            | 15 DAYS   | 0.28                            | 0.13       | 0.22       | 0.57       | 1.03       | 0.25                            | 0.28       | 0.16       | 0.47       | 0.91       |
|            | 20 DAYS   | 0.35                            | 0.20       | 0.25       | 0.86       | 1.90       | 0.32                            | 0.32       | 0.14       | 0.59       | 1.54       |
|            | 25 DAYS   | 0.38                            | 0.27       | 0.23       | 1.17       | 3.17       | 0.39                            | 0.36       | 0.21       | 0.72       | 2.39       |
|            | 30 DAYS   | 0.41                            | 0.32       | 0.30       | 1.54       | 5.00       | 0.28                            | 0.44       | 0.31       | 0.97       | 3.63       |

NOTE: THE RMS PREDICTION ERRORS ARE IN UNITS OF MICROSECONDS.

NUMBER OF SAMPLE INTERVALS

| PREDICTION | LEAD TIME | 7  | 14 | CALIBRATION INTERVAL |    |    | 56 |
|------------|-----------|----|----|----------------------|----|----|----|
|            |           |    |    | 21                   | 28 | 42 |    |
| DAY        | 1         | 53 | 32 | 20                   | 15 | 3  | 3  |
|            | 2         | 63 | 32 | 20                   | 15 | 3  | 8  |
|            | 5         | 63 | 32 | 20                   | 15 | 3  | 8  |
|            | 10        | 63 | 32 | 20                   | 15 | 3  | 9  |
|            | 15        | 54 | 32 | 18                   | 12 | 7  | 8  |
|            | 20        | 62 | 33 | 18                   | 12 | 7  | 3  |
|            | 25        | 53 | 27 | 13                   | 10 | 7  | 3  |
|            | 30        | 57 | 25 | 15                   | ?  | 7  | 7  |

TABLE 17  
RMS PREDICTION ERRORS  
FOR  
OSCILLATING CESIUM FREQUENCY OSCILLATOR #58  
MODIFIED JULIAN DAY: 4+120 - 4+350

| PREDICTION<br>LEAD TIME | ARIMA | CALIBRATION INTERVAL<br>7 DAYS  |            |            |            |       | CALIBRATION INTERVAL<br>14 DAYS |            |            |            |      |
|-------------------------|-------|---------------------------------|------------|------------|------------|-------|---------------------------------|------------|------------|------------|------|
|                         |       | 1ST DEGREE                      | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA | 1ST DEGREE                      | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |      |
| 1 DAY                   | 0.02  | 0.02                            | 0.02       | 0.02       | 0.04       | 0.01  | 0.03                            | 0.02       | 0.03       | 0.03       | 0.03 |
| 2 DAYS                  | 0.03  | 0.03                            | 0.04       | 0.05       | 0.12       | 0.03  | 0.04                            | 0.04       | 0.05       | 0.05       | 0.05 |
| 5 DAYS                  | 0.10  | 0.05                            | 0.11       | 0.33       | 1.11       | 0.07  | 0.06                            | 0.07       | 0.14       | 0.31       |      |
| 10 DAYS                 | 0.23  | 0.09                            | 0.30       | 1.50       | 3.71       | 0.17  | 0.10                            | 0.15       | 0.47       | 1.55       |      |
| 15 DAYS                 | 0.54  | 0.14                            | 0.58       | 4.06       | 33.10      | 0.31  | 0.15                            | 0.26       | 1.08       | 4.84       |      |
| 20 DAYS                 | 0.89  | 0.20                            | 0.95       | 8.54       | 90.05      | 0.50  | 0.20                            | 0.41       | 2.11       | 11.63      |      |
| 25 DAYS                 | 1.31  | 0.25                            | 1.42       | 15.62      | 200.91     | 0.75  | 0.25                            | 0.59       | 3.36       | 23.91      |      |
| 30 DAYS                 | 1.83  | 0.32                            | 1.93       | 34.91      | 362.05     | 1.05  | 0.30                            | 0.77       | 5.11       | 40.60      |      |
| PREDICTION<br>LEAD TIME | ARIMA | CALIBRATION INTERVAL<br>21 DAYS |            |            |            |       | CALIBRATION INTERVAL<br>28 DAYS |            |            |            |      |
|                         |       | 1ST DEGREE                      | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA | 1ST DEGREE                      | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |      |
| 1 DAY                   | 0.01  | 0.03                            | 0.02       | 0.02       | 0.02       | 0.02  | 0.03                            | 0.03       | 0.02       | 0.03       | 0.03 |
| 2 DAYS                  | 0.02  | 0.04                            | 0.04       | 0.03       | 0.04       | 0.03  | 0.04                            | 0.04       | 0.04       | 0.05       |      |
| 5 DAYS                  | 0.06  | 0.06                            | 0.07       | 0.08       | 0.15       | 0.05  | 0.06                            | 0.07       | 0.07       | 0.15       |      |
| 10 DAYS                 | 0.13  | 0.10                            | 0.13       | 0.23       | 0.59       | 0.12  | 0.11                            | 0.15       | 0.17       | 0.43       |      |
| 15 DAYS                 | 0.23  | 0.15                            | 0.22       | 0.48       | 1.53       | 0.20  | 0.16                            | 0.25       | 0.33       | 1.15       |      |
| 20 DAYS                 | 0.37  | 0.22                            | 0.34       | 0.89       | 3.31       | 0.30  | 0.22                            | 0.34       | 0.59       | 2.37       |      |
| 25 DAYS                 | 0.52  | 0.23                            | 0.49       | 1.45       | 5.09       | 0.41  | 0.26                            | 0.45       | 0.76       | 4.27       |      |
| 30 DAYS                 | 0.70  | 0.34                            | 0.64       | 2.17       | 10.51      | 0.53  | 0.30                            | 0.50       | 1.44       | 7.13       |      |
| PREDICTION<br>LEAD TIME | ARIMA | CALIBRATION INTERVAL<br>42 DAYS |            |            |            |       | CALIBRATION INTERVAL<br>56 DAYS |            |            |            |      |
|                         |       | 1ST DEGREE                      | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE | ARIMA | 1ST DEGREE                      | 2ND DEGREE | 3RD DEGREE | 4TH DEGREE |      |
| 1 DAY                   | 0.02  | 0.04                            | 0.04       | 0.03       | 0.03       | 0.01  | 0.07                            | 0.05       | 0.04       | 0.03       | 0.03 |
| 2 DAYS                  | 0.02  | 0.05                            | 0.05       | 0.04       | 0.05       | 0.02  | 0.07                            | 0.06       | 0.05       | 0.05       |      |
| 5 DAYS                  | 0.04  | 0.07                            | 0.09       | 0.07       | 0.10       | 0.04  | 0.09                            | 0.08       | 0.09       | 0.11       |      |
| 10 DAYS                 | 0.09  | 0.03                            | 0.16       | 0.15       | 0.27       | 0.08  | 0.12                            | 0.14       | 0.19       | 0.23       |      |
| 15 DAYS                 | 0.15  | 0.12                            | 0.26       | 0.25       | 0.58       | 0.13  | 0.16                            | 0.20       | 0.33       | 0.55       |      |
| 20 DAYS                 | 0.23  | 0.15                            | 0.33       | 0.36       | 1.11       | 0.20  | 0.20                            | 0.25       | 0.50       | 0.98       |      |
| 25 DAYS                 | 0.32  | 0.20                            | 0.41       | 0.54       | 1.91       | 0.27  | 0.26                            | 0.31       | 0.70       | 1.60       |      |
| 30 DAYS                 | 0.43  | 0.23                            | 0.52       | 0.75       | 3.05       | 0.38  | 0.28                            | 0.36       | 0.97       | 2.34       |      |

NOTE: THE RMS PREDICTION ERRORS ARE IN UNITS OF MICROSECONDS.

NUMBER OF SAMPLE INTERVALS

| PREDICTION<br>LEAD TIME | 7   | 14 | CALIBRATION INTERVAL |    |    | 56 |
|-------------------------|-----|----|----------------------|----|----|----|
|                         |     |    | 21                   | 23 | 42 |    |
| DAY 1                   | 132 | 6+ | ++                   | 32 | 20 | 16 |
| 2                       | 132 | 64 | ++                   | 32 | 20 | 16 |
| 5                       | 132 | 64 | 44                   | 32 | 20 | 15 |
| 10                      | 132 | 63 | 44                   | 31 | 20 | 16 |
| 15                      | 130 | 51 | 43                   | 31 | 20 | 16 |
| 20                      | 129 | 59 | 42                   | 30 | 20 | 16 |
| 25                      | 129 | 55 | 41                   | 29 | 20 | 16 |
| 30                      | 122 | 52 | 40                   | 29 | 20 | 15 |

TABLE 18  
RMS PREDICTION ERRORS  
FOR  
HYDROGEN MASER #10  
MODIFIED JULIAN DAY: 43970 - 44023

| PREDICTION<br>LEAD TIME | ARIMA | CALIBRATION INTERVAL<br>7 DAYS  |               |               |               |       | CALIBRATION INTERVAL<br>14 DAYS |               |               |               |  |
|-------------------------|-------|---------------------------------|---------------|---------------|---------------|-------|---------------------------------|---------------|---------------|---------------|--|
|                         |       | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE | ARIMA | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE |  |
| 1 DAY                   | 0.01  | 0.02                            | 0.02          | 0.02          | 0.03          | 0.01  | 0.03                            | 0.01          | 0.02          | 0.02          |  |
| 2 DAYS                  | 0.03  | 0.03                            | 0.03          | 0.05          | 0.11          | 0.01  | 0.05                            | 0.02          | 0.03          | 0.03          |  |
| 5 DAYS                  | 0.08  | 0.09                            | 0.09          | 0.25          | 0.97          | 0.05  | 0.11                            | 0.04          | 0.07          | 0.36          |  |
| 10 DAYS                 | 0.20  | 0.15                            | 0.25          | 1.17          | 7.34          | 0.11  | 0.21                            | 0.37          | 0.25          | 1.24          |  |
| 15 DAYS                 | 0.38  | 0.29                            | 0.45          | 3.05          | 23.70         | 0.22  | 0.38                            | 0.10          | 0.54          | 5.74          |  |
| 20 DAYS                 | 0.57  | 0.44                            | 0.64          | 6.49          | 79.26         | 0.28  | 0.60                            | 0.10          | 0.64          | 11.18         |  |
| 25 DAYS                 | 0.91  | 0.60                            | 0.92          | 12.24         | 173.46        | 0.39  | 0.84                            | 0.15          | 1.09          | 22.57         |  |
| 30 DAYS                 | 1.20  | 0.93                            | 1.27          | 18.29         | 365.65        | 0.75  | 1.14                            | 0.17          | 2.34          | 41.95         |  |
| PREDICTION<br>LEAD TIME | ARIMA | CALIBRATION INTERVAL<br>21 DAYS |               |               |               |       | CALIBRATION INTERVAL<br>28 DAYS |               |               |               |  |
|                         |       | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE | ARIMA | 1ST<br>DEGREE                   | 2ND<br>DEGREE | 3RD<br>DEGREE | 4TH<br>DEGREE |  |
| 1 DAY                   | 0.31  | 0.03                            | 0.02          | 0.02          | 0.02          | 0.01  | 0.12                            | 0.02          | 0.02          | 0.02          |  |
| 2 DAYS                  | 0.02  | 0.13                            | 0.03          | 0.04          | 0.03          | 0.03  | 0.15                            | 0.03          | 0.03          | 0.04          |  |
| 5 DAYS                  | 0.04  | 0.17                            | 0.05          | 0.07          | 0.13          | 0.07  | 0.23                            | 0.05          | 0.05          | 0.13          |  |
| 10 DAYS                 | 0.10  | 0.33                            | 0.07          | 0.16          | 0.56          | 0.12  | 0.42                            | 0.07          | 0.11          | 0.38          |  |
| 15 DAYS                 | 0.19  | 0.52                            | 0.09          | 0.35          | 1.27          | 0.18  | 0.64                            | 0.07          | 0.20          | 0.95          |  |
| 20 DAYS                 | 0.12  | 0.74                            | 0.19          | 0.76          | 2.52          | 0.19  | 0.90                            | 0.06          | 0.24          | 1.58          |  |
| 25 DAYS                 | 0.08  | 1.05                            | 0.26          | 1.38          | 5.29          | 0.17  | 1.21                            | 0.13          | 0.63          | 1.19          |  |
| 30 DAYS                 | 0.10  | 1.30                            | 0.33          | 2.03          | 9.09          | ----  | ----                            | ----          | ----          | ----          |  |

NOTE: THE RMS PREDICTION ERRORS ARE IN UNITS OF MICROSECONDS.

| PREDICTION<br>LEAD TIME | 7  | NUMBER OF SAMPLE INTERVALS |    |    |      |
|-------------------------|----|----------------------------|----|----|------|
|                         |    | CALIBRATION INTERVAL       | 14 | 21 | 28   |
| DAY                     | 1  | 32                         | 10 | 9  | 8    |
|                         | 2  | 32                         | 16 | 8  | 3    |
|                         | 5  | 32                         | 16 | 8  | 3    |
|                         | 10 | 31                         | 15 | 8  | 3    |
|                         | 15 | 27                         | 15 | 6  | 5    |
|                         | 20 | 25                         | 13 | 4  | 3    |
|                         | 25 | 23                         | 12 | 3  | 1    |
|                         | 30 | 13                         | 4  | 3  | ---- |

TABLE 19  
RMS PREDICTION ERRORS  
FOR  
QUARTZ-MATIC 31  
MODIFIED JULIAN DAY: 43730 - 44040

| PREDICTION<br>LEAD TIME | ARIMA | CALIBRATION INTERVAL |            |            | CALIBRATION INTERVAL |            |            |
|-------------------------|-------|----------------------|------------|------------|----------------------|------------|------------|
|                         |       | 7 DAYS               | 21 DAYS    | 42 DAYS    | 14 DAYS              | 28 DAYS    | 56 DAYS    |
|                         |       | 2ND DEGREE           | 3RD DEGREE | 4TH DEGREE | 2ND DEGREE           | 3RD DEGREE | 4TH DEGREE |
| 1 DAY                   | .313  | .020                 | .024       | .038       | 0.015                | 0.032      | 0.036      |
| 2 DAYS                  | .035  | .043                 | .072       | .137       | 0.034                | 0.055      | 0.069      |
| 5 DAYS                  | .125  | .135                 | .391       | 1.231      | 0.095                | 0.134      | 0.215      |
| 10 DAYS                 | .373  | .391                 | 1.782      | 9.564      | 0.244                | 0.320      | 0.709      |
| 15 DAYS                 | .740  | .772                 | 4.304      | 36.326     | 0.474                | 0.596      | 1.462      |
| 20 DAYS                 | 1.109 | 1.147                | 9.735      | 98.021     | 0.731                | 0.892      | 2.792      |
| 25 DAYS                 | 1.670 | 1.723                | 17.645     | 217.230    | 1.149                | 1.274      | 4.740      |
| 30 DAYS                 | 2.373 | 2.444                | 29.075     | 423.963    | 1.600                | 1.769      | 7.451      |

| PREDICTION<br>LEAD TIME | ARIMA | CALIBRATION INTERVAL |            |            | CALIBRATION INTERVAL |            |            |
|-------------------------|-------|----------------------|------------|------------|----------------------|------------|------------|
|                         |       | 2ND DEGREE           | 3RD DEGREE | 4TH DEGREE | 2ND DEGREE           | 3RD DEGREE | 4TH DEGREE |
| 1 DAY                   | .313  | .042                 | .033       | .033       | 0.012                | 0.053      | 0.041      |
| 2 DAYS                  | .038  | .063                 | .057       | .069       | 0.029                | 0.078      | 0.065      |
| 5 DAYS                  | .092  | .120                 | .129       | .233       | 0.078                | 0.161      | 0.161      |
| 10 DAYS                 | .257  | .313                 | .395       | .909       | 0.197                | 0.334      | 0.422      |
| 15 DAYS                 | .477  | .559                 | .333       | 2.442      | 0.399                | 0.560      | 0.737      |
| 20 DAYS                 | .721  | .858                 | 1.530      | 9.259      | 0.646                | 0.848      | 1.358      |
| 25 DAYS                 | 1.032 | 1.200                | 2.546      | 10.141     | 0.941                | 1.192      | 2.114      |
| 30 DAYS                 | 1.403 | 1.602                | 3.917      | 17.657     | 1.284                | 1.583      | 3.109      |

| PREDICTION<br>LEAD TIME | ARIMA | CALIBRATION INTERVAL |            |            | CALIBRATION INTERVAL |            |            |
|-------------------------|-------|----------------------|------------|------------|----------------------|------------|------------|
|                         |       | 2ND DEGREE           | 3RD DEGREE | 4TH DEGREE | 2ND DEGREE           | 3RD DEGREE | 4TH DEGREE |
| 1 DAY                   | .313  | .086                 | .087       | .044       | 0.016                | 0.132      | 0.085      |
| 2 DAYS                  | .031  | .114                 | .123       | .067       | 0.035                | 0.159      | 0.107      |
| 5 DAYS                  | .094  | .213                 | .241       | .170       | 0.093                | 0.244      | 0.188      |
| 10 DAYS                 | .169  | .393                 | .471       | .473       | 0.239                | 0.439      | 0.356      |
| 15 DAYS                 | .317  | .626                 | .720       | 1.163      | 0.416                | 0.648      | 0.577      |
| 20 DAYS                 | .503  | .345                 | 1.025      | 2.289      | 0.633                | 0.907      | 0.878      |
| 25 DAYS                 | .735  | 1.142                | 1.454      | 4.142      | 0.872                | 1.191      | 1.230      |
| 30 DAYS                 | 1.313 | 1.465                | 1.979      | 6.059      | 1.223                | 1.541      | 1.715      |

NOTE: THE RMS PREDICTION ERRORS ARE IN UNITS OF SECONDS.

| PREDICTION<br>LEAD TIME | 7   | 14 | NUMBER OF SAMPLE INTERVALS |    |    |    |
|-------------------------|-----|----|----------------------------|----|----|----|
|                         |     |    | CALIBRATION INTERVAL       | 21 | 28 | 42 |
| 1 DAY                   | 160 | 38 | 50                         | 44 | 23 | 23 |
| 2                       | 180 | 33 | 60                         | 44 | 23 | 20 |
| 5                       | 180 | 33 | 60                         | 43 | 23 | 20 |
| 10                      | 180 | 33 | 50                         | 41 | 25 | 20 |
| 15                      | 177 | 35 | 50                         | 41 | 25 | 20 |
| 20                      | 177 | 84 | 57                         | 41 | 23 | 20 |
| 25                      | 175 | 84 | 57                         | 41 | 23 | 17 |
| 30                      | 173 | 33 | 55                         | 41 | 23 |    |

FIGURE 16

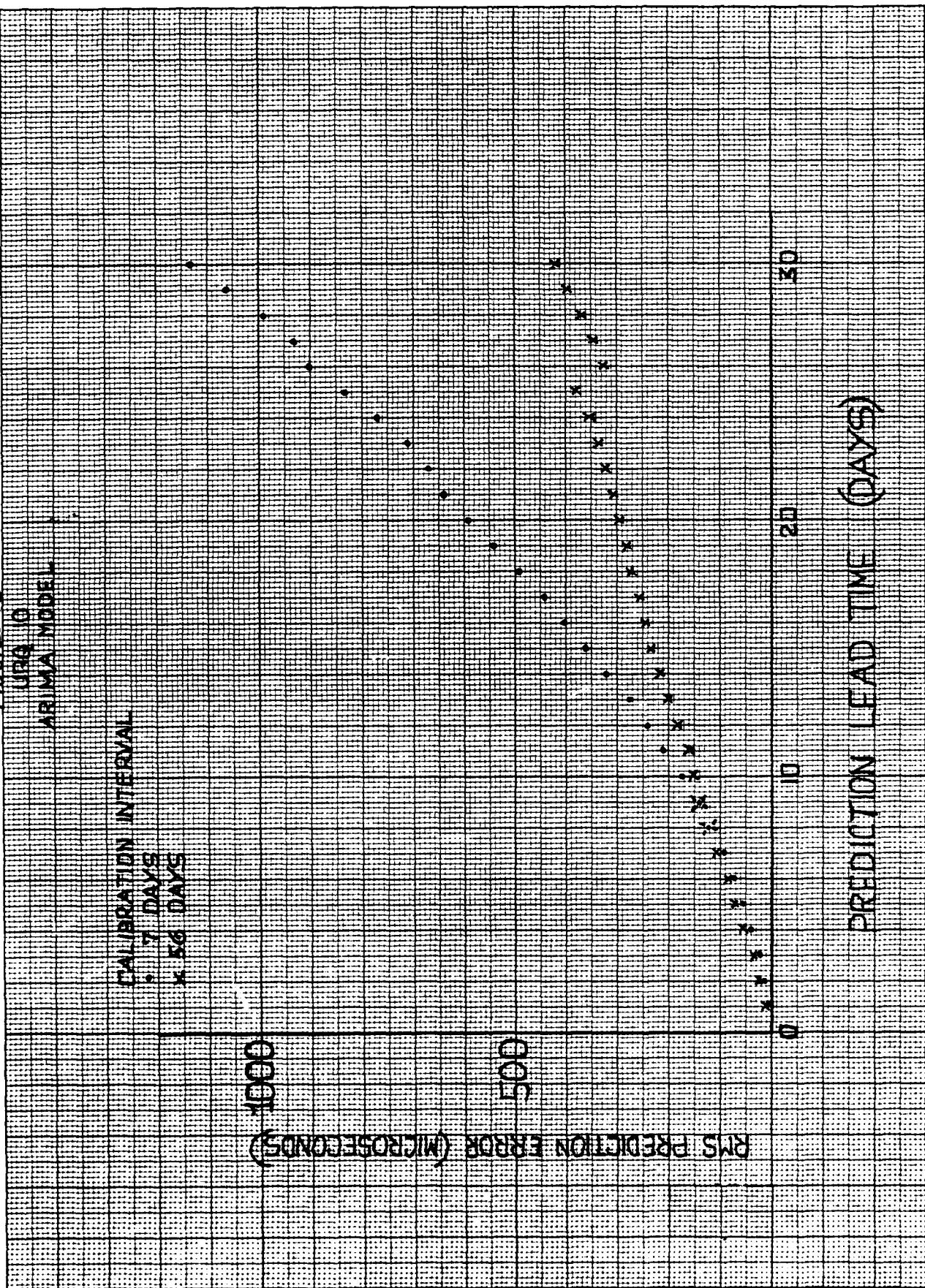
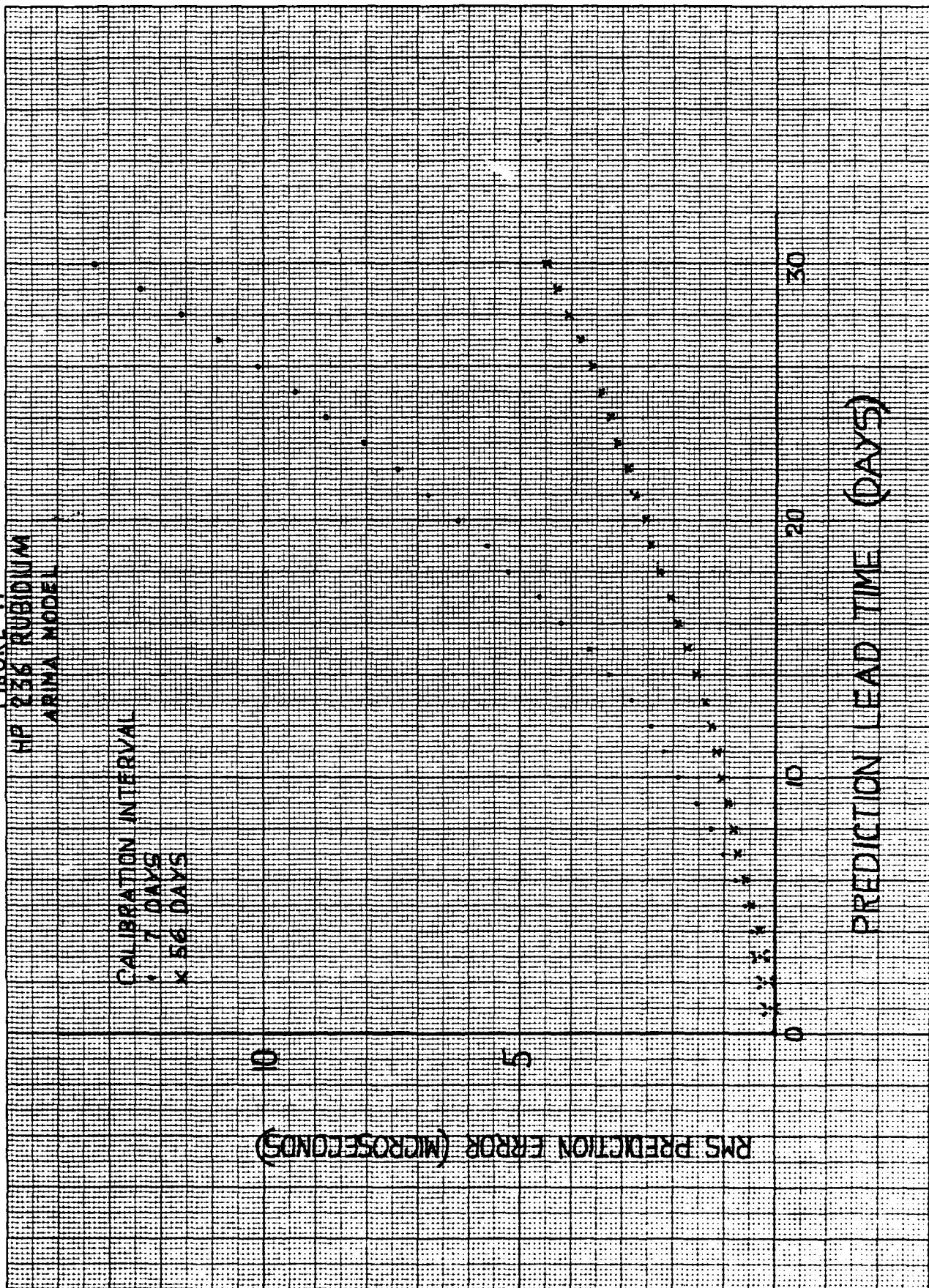


FIGURE 17  
HF 238 RUBIDIUM  
ARMA MODEL



## Appendix A.1

### DISCIPLINED TIME FREQUENCY OSCILLATOR\*

## TECHNICAL SPECIFICATIONS

### OUTPUT SIGNALS

#### FREQUENCIES

|              |               |
|--------------|---------------|
| Sine Wave:   | 5 MHz, 1 MHz  |
| Square Wave: | 100 kHz       |
| Pulse:       | 1 PPS, 1 MPPS |

#### LEVELS:

|              |                                                                                                                 |
|--------------|-----------------------------------------------------------------------------------------------------------------|
| Sine Wave:   | 1.0 Vrms $\pm 20\%$ into 50 ohms                                                                                |
| Square Wave: | TTL compatible, 50% duty cycle                                                                                  |
| Pulse:       |                                                                                                                 |
| 1 PPS:       | +4.7 V $\pm 10\%$ into 50 ohm, 20 usec. wide. Rise time less than 10ns. Jitter less than 100ps (unsynchronized) |
| 1 MPPS       | 0.2 usec. wide, negative going, TTL compatible                                                                  |

#### STABILITY (5 MHz):

##### AVERAGING TIME:

|                              |                                                            |
|------------------------------|------------------------------------------------------------|
| 100 usec.                    | 3 PP10 <sup>9</sup>                                        |
| 1 msec.                      | 4 PP10 <sup>10</sup>                                       |
| 10 msec.                     | 5 PP10 <sup>11</sup>                                       |
| 100 msec.                    | 6 PP10 <sup>12</sup>                                       |
| 1 sec.                       | 2 PP10 <sup>12</sup>                                       |
| 10 sec.                      | 2 PP10 <sup>12</sup>                                       |
| 100 sec.                     | 3 PP10 <sup>12</sup>                                       |
| 24 Hours:                    | 3.5 PP10 <sup>11</sup>                                     |
| Under shock<br>(MIL-E-16400) | 2 PP10 <sup>9</sup>                                        |
| Temperature<br>(0° to +50°C) | 2 PP10 <sup>10</sup>                                       |
| Orientation                  | $\Delta f/f \pm 5 \text{ PP10}^{10}$ max at $\pm 45^\circ$ |

**ISOLATION:** All outputs short circuit proof.  
1 PP 10<sup>11</sup> freq change no load to full load.

#### SPECTRAL PURITY:

Harmonics: <-40 dB

Spurious: 5 MHz, 1 MHz < -110 dB

| Noise | Frequency<br>From Carrier | Single Sideband<br>Noise (dB/Hz).<br>Referenced to<br>Carrier |       |
|-------|---------------------------|---------------------------------------------------------------|-------|
|       |                           | 5 MHz                                                         | 1 MHz |
|       | 10 Hz                     | -130                                                          | -135  |
|       | 100 Hz                    | -140                                                          | -140  |
|       | 1 kHz                     | -160                                                          | -145  |
|       | 10 kHz                    | -165                                                          | -150  |

#### WARM-UP CHARACTERISTIC (at +22°C)

|                              |          |
|------------------------------|----------|
| To lock                      | <1 hour  |
| To 5 PP10 <sup>11</sup> /day | <11 days |

#### OSCILLATOR ADJUSTMENT

|                    |                                                     |
|--------------------|-----------------------------------------------------|
| Coarse Adj. Range: | 1 PP 10 <sup>9</sup>                                |
| Fine Adj. Range:   | Digital Indicator 0 to 999<br>in PP10 <sup>11</sup> |

\*Excerpt from Reference 7

### PHASE LOCK FUNCTIONS

#### INPUT FREQUENCIES:

|       |          |
|-------|----------|
| 5 MHz | 1-10V PP |
| 1 MHz | 1-4V PP  |

#### INPUT IMPEDANCE:

>1000 ohms

#### RESOLUTION (With Memory):

$\pm 2.5 \text{ PP10}^{12}$

#### PHASE LOCK LOOP FILTER:

|                |                                        |
|----------------|----------------------------------------|
| Time Constant: | 100 sec. or 1 sec., switch selectable. |
| Control Range: | $\pm 1 \text{ PP10}^8$                 |

#### UNLOCK DETECTOR:

Responds to loss of input signal level, phase detector slippage, or loss of internal reference

#### LOCK ACQUISITION:

Manual control.

### 1 PPS GENERATOR

#### SYNCHRONIZATION INPUT:

- a) 1 PPS, 1-10V PP width >5 usec.
- b) 1 PPS +1 MHz (Algebraically added) equal amplitudes of 1-3V PP, pulse width >5 usec.
- c) Sync Pulse Rise Time: 0.1 usec. maximum

#### Synchronization Delay:

0.5 usec. min., 0.25 usec. max.

#### Synchronization Mode:

- a) Continuous (Syncs to every input pulse)
- b) Intermittent (Syncs to first pulse after switch is thrown)

### POWER REQUIREMENTS:

AC: 115 Vac  $\pm 10\%$ , 50-400 Hz, single phase (15 watts nominal) 28 watts max.

External DC: +22 to +30 Vdc (12 watts nominal) 26 watts max. (cold start)

Internal Battery Capacity: 7 hours at +22°C (automatic recharge)

## CIRCUIT CHECK FUNCTIONS

### TEST METER/SWITCH

Front Panel Switch:  
12 Positions  
5 MHz output  
1 MHz output  
100 kHz output  
Memory Voltage  
5 MHz or 1 MHz  
Reference Input  
Battery Charge/Discharge Current  
Battery Voltage  
+10 VDC  
DC Input  
Outer Oven Monitor  
Regulator Voltage  
Inner Oven Monitor

## CONNECTORS

Front and Rear: 5 MHz, 1 MHz, 100 kHz,  
1 PPS (BNC)  
Front Only: 1 PPS sync input (BNC)  
5 MHz lock input (BNC)  
Rear Only: 1 MHz +1 PPS sync and lock  
input, 1 MPPS output, (BNC)  
EXT. DC input.  
(MS 3102E-10SL-3P)

## ENVIRONMENTAL

Humidity: 95% RH  
Altitude: 0 to 15000 ft.  
Operating Temperature Range: 0°C to +50°C (Navy Class 3)  
Shock & Vibration: Per MIL-E-16400  
(Note: to MIL-E-5400 optional)  
EMI Meets MIL-STD-461.  
MIL-STD-462.

## MECHANICAL

Portable: Carrying handle integral to case.  
Housing Dimensions: 12" long x 5 1/2" wide x 7 3/4" high  
Weight w/Batteries: 23 pounds

## OPTIONS:

- 1) Phase lock input for 1/N MHz rate, all integral submultiples of 1 MHz from 500 kHz down to 1 Hz.
- 2) Other operating temperature ranges (-54°C to +65°C, -40°C to +55°C, +15°C to +35°C, Navy classes 1, 2, 4 respectively).
- 3) 10 minutes warmup to lock.
- 4) DTF Module FE 150A may be ordered separately for OEM users (See outline drawing for installation details).
- 5) DTF without 1 PPS Generator and Frequency Control is a low noise high stability standard.
- 6) Additional Battery Pack for extended battery operating periods up to 24 hours.
- 7) MIL-E-5400 environmental specification.
- 8) AC failure remote alarm relay.
- 9) Permanent non-volatile memory for restoration of DTF accuracy after complete power failure.
- 10) Other output frequencies available.
- 11) External Memory "Hold" Control.
- 12) 100 MHz Output Module

## APPLICATIONS:

- 1) Quartz Crystal Frequency and Time Standard for laboratory, factory, ground and satellite communications, air collision avoidance or navigation systems.
- 2) Tracking Filter — Narrowband tracking filter (1 Hz or 0.01 Hz bandwidth).
- 3) Time clean-up filter. Synchronized at user's option, 50 pico-sec. jitter when unsynced.
- 4) Portable Time/Frequency Transfer. Sync the DTF to an Atomic Standard and transport to site for transfer or comparison of time-frequency.
- 5) Local or remote slave clean-up oscillator for cesium beam standard provides better short term stability characteristic and spectral purity.
- 6) Low noise carrier generator for exciting transmitters.
- 7) Low-noise reference for signal measurements.
- 8) Redundant clock with cesium standard, two DTF's plus cesium replaces three cesium standards and comparators.
- 9) Terminus of TV time link where information is intermittent.
- 10) Terminus of microwave link where information is intermittent.
- 11) Observation of unfiltered phase detector output enables measurement of jitter, spurious, etc. on other equipment.
- 12) Portable accurate time transfer for line delay measurements.

Appendix A.2  
OSCILLOQUARTZ\*

3.0 Performance. Equipment performances established by this specification are minimum requirements, and any variations must only be in the direction of improved performance. The contractor is held responsible for meeting these performance requirements unless specific exception has been obtained in writing from the Contracting Officer.

3.1 Output Signals.

Sine Wave                            1 MHz and 5 MHz at 1.0 V<sub>rms</sub> ±20%  
                                        into 50 ohms

Pulse                                1 PPS at 5V PP ±20% into 50 ohms

3.2 Frequency Stability.  $\frac{\Delta f}{f}$  -5 MHz Signal (Under free-running and memory conditions)

Averaging Time                     $\frac{\Delta f}{f}$

10 msec                              5 in 10<sup>11</sup>

100 msec                            6 in 10<sup>12</sup>

1 sec                                2 in 10<sup>12</sup>

100 sec                             3 in 10<sup>12</sup>

Frequency Drift. After a warm-up period of 10 days, the accumulated frequency drift shall not exceed the following rates:

24 hours                            1 in 10<sup>10</sup>

10 days                            7 in 10<sup>10</sup>

Environmental Effects. The frequency errors caused by the following effects shall not exceed the following:

Temperature (0° to 50°C)        ±5 in 10<sup>10</sup>

Supply Voltage  
(115 VAC ±10%)                ±3 in 10<sup>11</sup>

Load Variation  
(50 ohms ±10%)                ±5 in 10<sup>11</sup>

Orientation (±45°)                ±5 in 10<sup>10</sup>

\*Excerpt from Solicitation No. N68171-76-R-0144, 13 April 1976.

### 3.3 Spectral Purity.

- (a) Harmonics                            5 MHz - At least 40 dB below output  
                                              1 MHz - At least 30 dB below output
- (b) Non-Harmonic, Subharmonics, & Spurious                    5 MHz - At least 110 dB below output for frequency offset greater than 1000 Hz from carrier.

### (c) Single Sideband Noise (dB/Hz)

| <u>Frequency Offset from Carrier (Hz)</u> | <u>5 MHz</u> | <u>1 MHz</u> |
|-------------------------------------------|--------------|--------------|
| 0.1                                       | -71          | -76          |
| 1                                         | -101         | -106         |
| 10                                        | -130         | -135         |
| 100                                       | -140         | -140         |
| 1000                                      | -160         | -145         |

### 3.4 Frequency Adjustment.

- Coarse Adjustment Range                1 in  $10^7$   
Fine Adjustment Range                 1 in  $10^8$   
Resolution                              2 in  $10^{11}$

### 3.5 Phase Lock Function. The capability of being phase-locked to the following input reference frequencies shall be provided.

|                                |                                                                                         |
|--------------------------------|-----------------------------------------------------------------------------------------|
| 5 MHz                          | 1 to 10V PP                                                                             |
| 1 MHz                          | 1 to 4V PP                                                                              |
| Input Impedance                | 50 ohms                                                                                 |
| Loop Filter                    | Time constant selectable 1, 10, and 100 seconds                                         |
| Control Range                  | 1 in $10^8$                                                                             |
| Resolution (with memory)       | 1 in $10^{11}$                                                                          |
| Unlock Indicator               | Activated by loss of input signal, phase detector slippage, or loss of reference signal |
| Loop Control Voltage Indicator | To allow coarse adjustment of oscillator frequency                                      |

**3.6 Digital Memory.** Capable of maintaining the oscillator at its last phase-locked frequency for a period of at least 10 days after reference signal is lost. During the period of no reference signal, the frequency stability and spectral purity shall be as specified in Paragraphs 3.2 and 3.3 respectively. Reacquisition of phase lock shall be automatic after the reference signal is restored and shall be accomplished at a correction rate no greater than the oscillator loop time constant.

**3.7 Synchronous Counter.**

|                              |                                                                                                                                    |
|------------------------------|------------------------------------------------------------------------------------------------------------------------------------|
| <b>Output</b>                | 1 PPS at 5V PP                                                                                                                     |
| <b>Synchronization Input</b> | 1 PPS at 1 to 10V into 50 ohms                                                                                                     |
| <b>Synchronization Mode</b>  | Continuous (syncs to every pulse),<br>intermittent (to first pulse)                                                                |
| <b>Synchronization Delay</b> | The internal 1 PPS shall be capable of<br>being shifted in steps of 0.1 $\mu$ sec maximum<br>over a range of 10 $\mu$ sec minimum. |

**3.8 Clock.**

**Time Counter**

|                        |                                                                                         |
|------------------------|-----------------------------------------------------------------------------------------|
| <b>Display</b>         | Hours, minutes, and seconds                                                             |
| <b>Synchronization</b> | Internal 1 PPS operates clock and<br>can be synchronized to external<br>1 PPS reference |
| <b>Time Setting</b>    | Push-button for rapid time setting                                                      |

**Time Comparator**

|                        |                                        |
|------------------------|----------------------------------------|
| <b>Display</b>         | Digital display of measured $\Delta t$ |
| <b>Reference Input</b> | 1 PPS, 1 to 10V PP into 50 ohms        |
| <b>Resolution</b>      | 0.1 $\mu$ sec                          |

**3.9 Power.**

|                               |                                             |
|-------------------------------|---------------------------------------------|
| <b>Primary Power</b>          | 115 VAC $\pm 10\%$ , 50 to 400 Hz $\pm 5\%$ |
| <b>Standby Battery Supply</b> | 2 hours at +22°C (including clock)          |
|                               | Floating input                              |
|                               | Automatic recharge                          |

**3.10 Environmental Conditions.**

**3.10.1 Equipment Operating.** The equipments shall meet the performance of this specification while subjected to any of the following conditions or combinations thereof:

|                   |                                     |
|-------------------|-------------------------------------|
| Operation         | Continuous (24 hours per day)       |
| Temperature Range | 0 to 50°C                           |
| Humidity          | 5% to 95% RH over temperature range |
| Altitude          | 0 to 10,000 feet above sea level.   |

**3.10.2 Equipment Non-Operating.** The equipments - as packaged for storage, during transit, and in any non-operating configuration - shall be constructed to comply with the operational requirements of this specification after subjection to any of the following non-operating conditions:

|                   |                                                                                   |
|-------------------|-----------------------------------------------------------------------------------|
| Temperature       | -32°C to +40°C                                                                    |
| Altitude          | 0 to 40,000 feet above sea level                                                  |
| Salt Atmosphere   | As encountered in coastal service                                                 |
| Shock & Vibration | As encountered in military transportation via rail, truck, or fixed-wing aircraft |

## Appendix B

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